

# Entrainment and detrainment in EDMF

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# Outline

Entrainment/detrainment in EDMF

New: The dry convection part  
(implementation in Harmonie/Arome)

Not new: The moist part

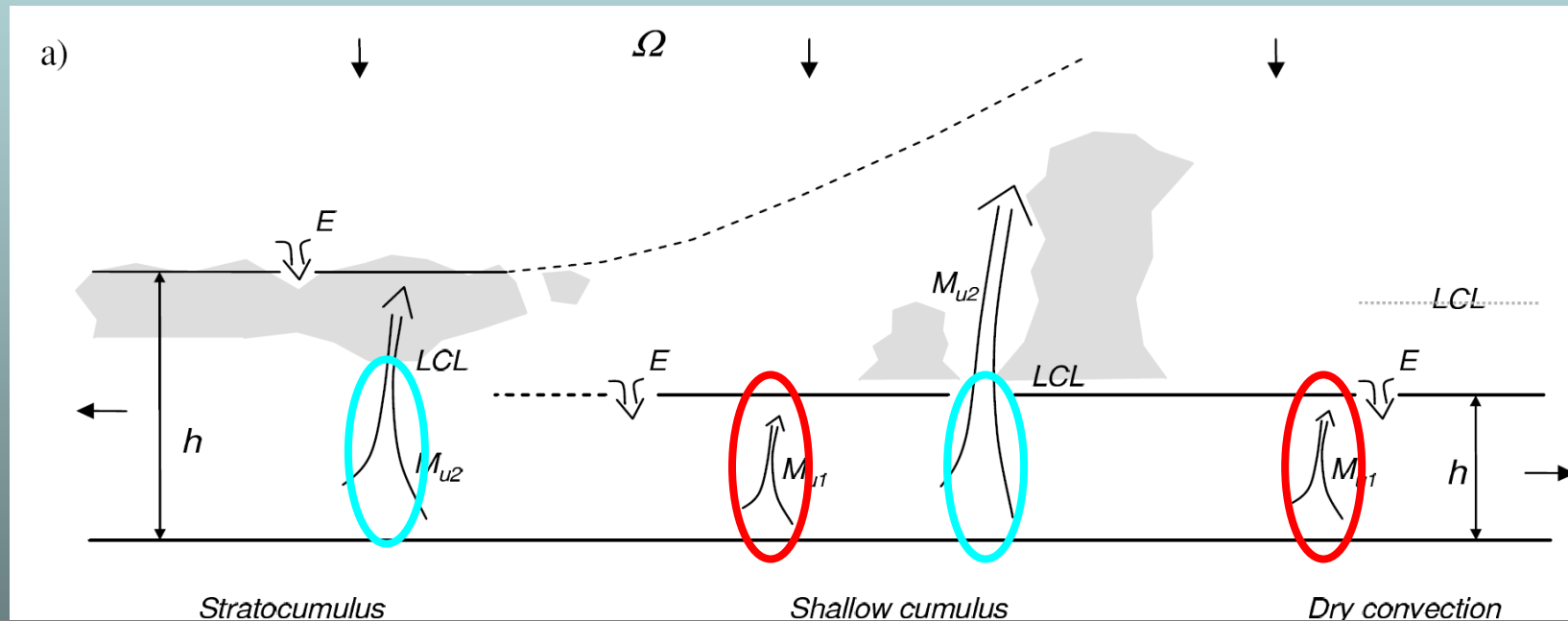
Traditional <-> Unconventional

Conclusions/recommendations

# Where dry?

## Dual mass flux framework (used in Harmonie)

*Roel Neggers et al. 2009*



Only moist updraft

Dry and moist updraft

Only dry updraft

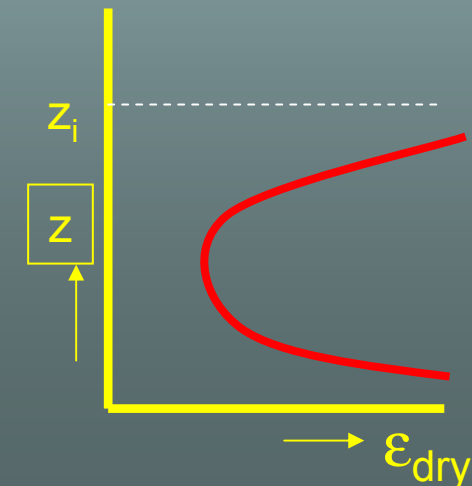
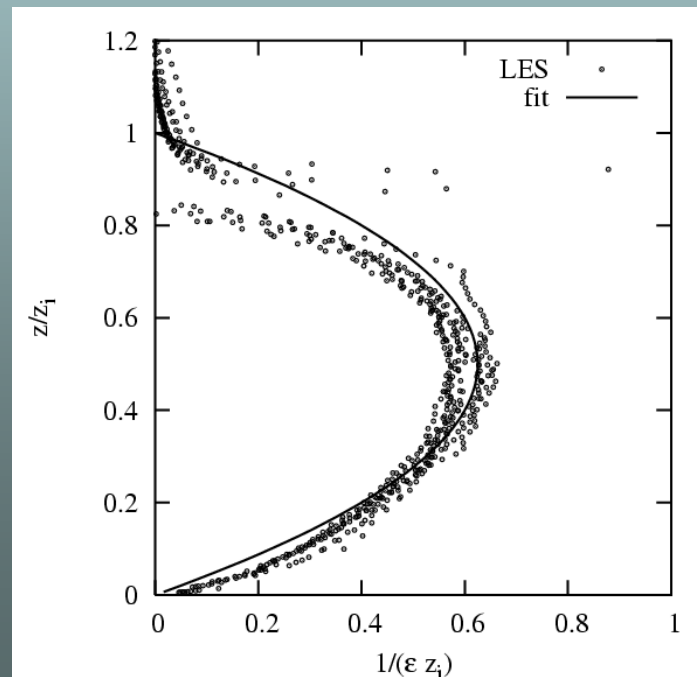
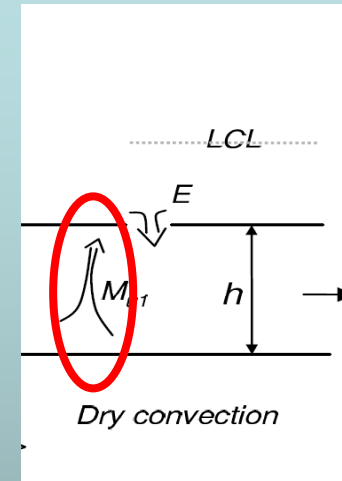
# Entrainment formulation for dry convective BL

Siebesma et al. 2007

Sampling based on percentile high w

$$\varepsilon = -\frac{\partial \theta_{lu}}{\partial z} / (\theta_{lu} - \bar{\theta}_l)$$

$$\varepsilon = c_e \left( \frac{1}{z} + \frac{1}{z_i - z} \right)$$



# Entrainment formulation for sub-cloud layer

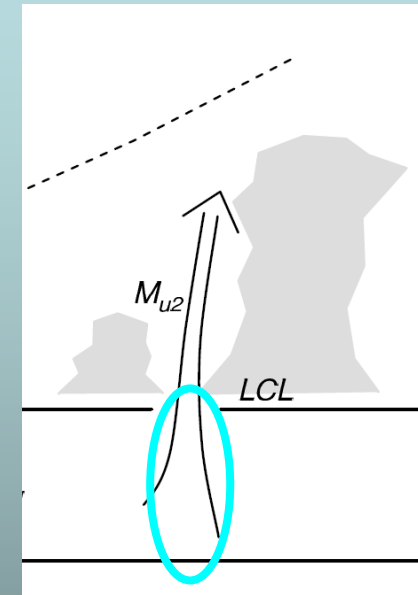
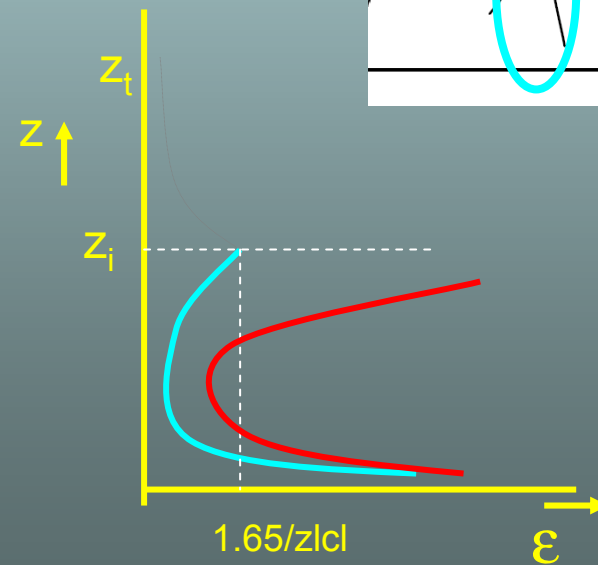
Difference with dry convective BL:

- Vertical velocity  $\neq 0$  for  $z=z_i$
- Stronger, bigger thermals (that can become cloud)

$\Rightarrow$  Building on the work of *Siebesma et al. 2007*

$$\varepsilon = 0.2 \left[ \frac{1}{z} + \frac{1}{z_{lcl} - z + \frac{0.2z_{lcl}}{1.45}} \right]$$

- Sub-cloud  $\varepsilon$
- Dry convection  $\varepsilon$



## Where is $\delta$ in the dry part?

Nowhere

Some simplifications:

In dry convection mass flux is determined by  $w_{\downarrow}$  (constant  $a$ )

In sub-cloud linked to mass flux closure at cloud base

## Entrainment and detrainment in the cloud layer

$\varepsilon$  and  $\delta$  have a different role

Continuity eq.: 
$$\frac{\partial M}{\partial z} = (\varepsilon - \delta)M$$

Entraining plume model: 
$$\frac{\partial \phi_u}{\partial z} = \varepsilon(\phi_u - \bar{\phi}) \quad \phi \in \{q_t, \theta_l\}$$

So:  
 $\varepsilon$  and  $\delta$  determine the mass flux profile  
and  
 $\varepsilon$  determines the dilution

# In the cloud layer

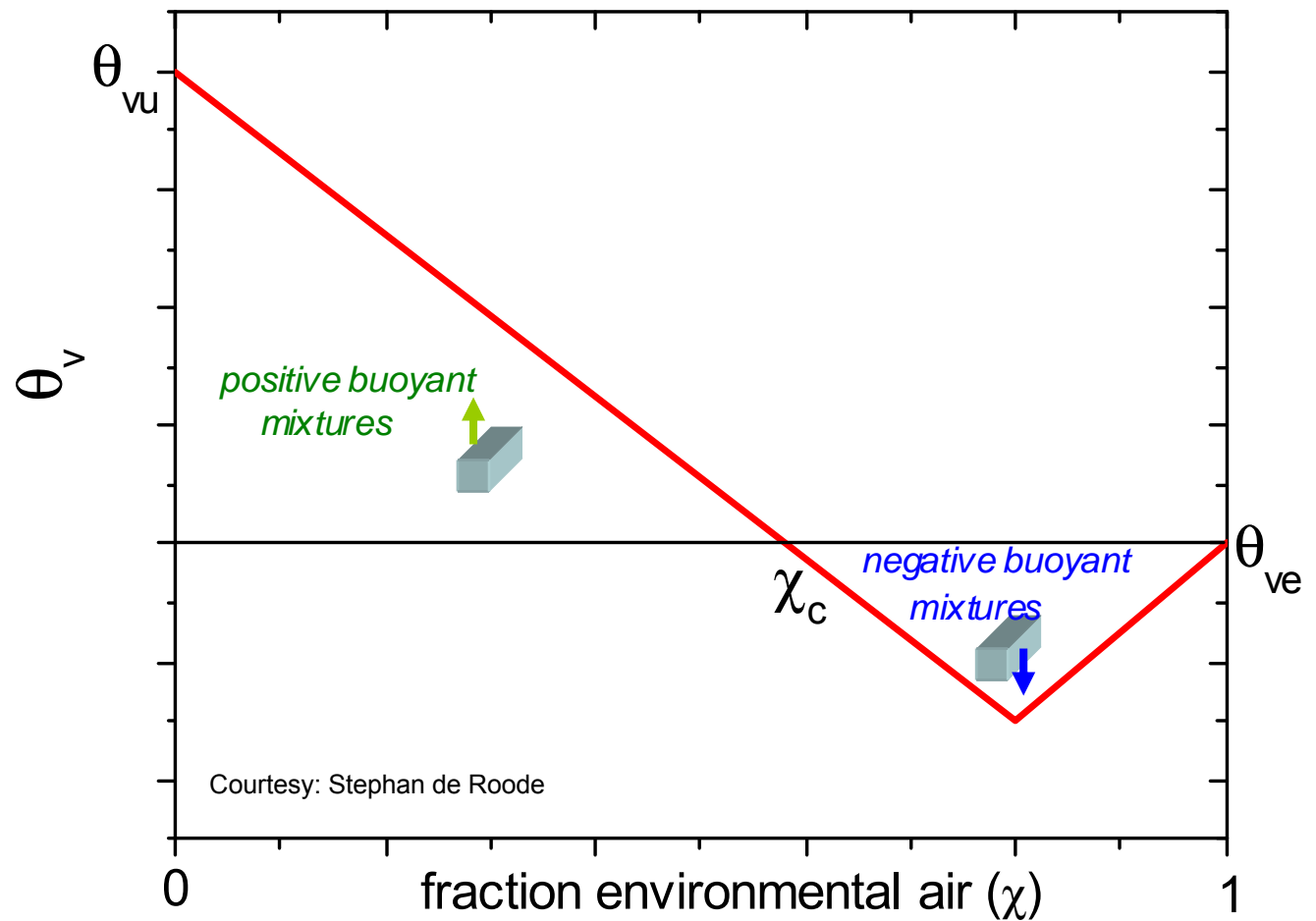
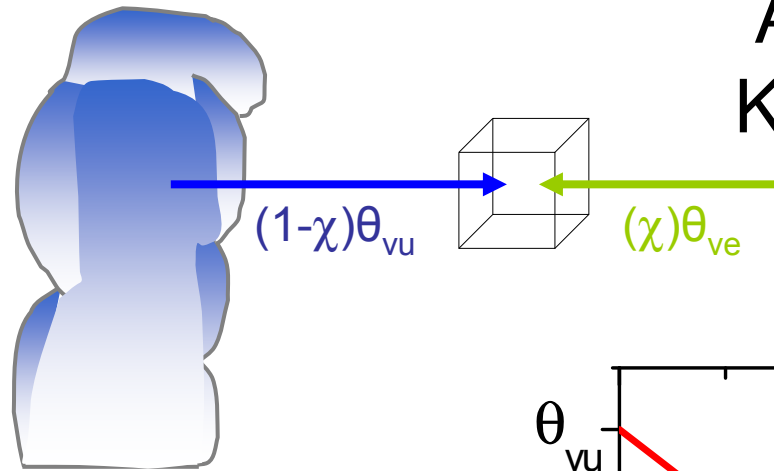
- Almost all convection (and EDMF) schemes prescribe some kind of function for  $\varepsilon$  and  $\delta$



Example of such a “traditional” scheme (Kain Fritsch)



# A popular traditional scheme: Kain Fritsch (buoyancy sorting)



# Kain Fritsch

- Several (tunable) parameters have to be chosen but in principle:

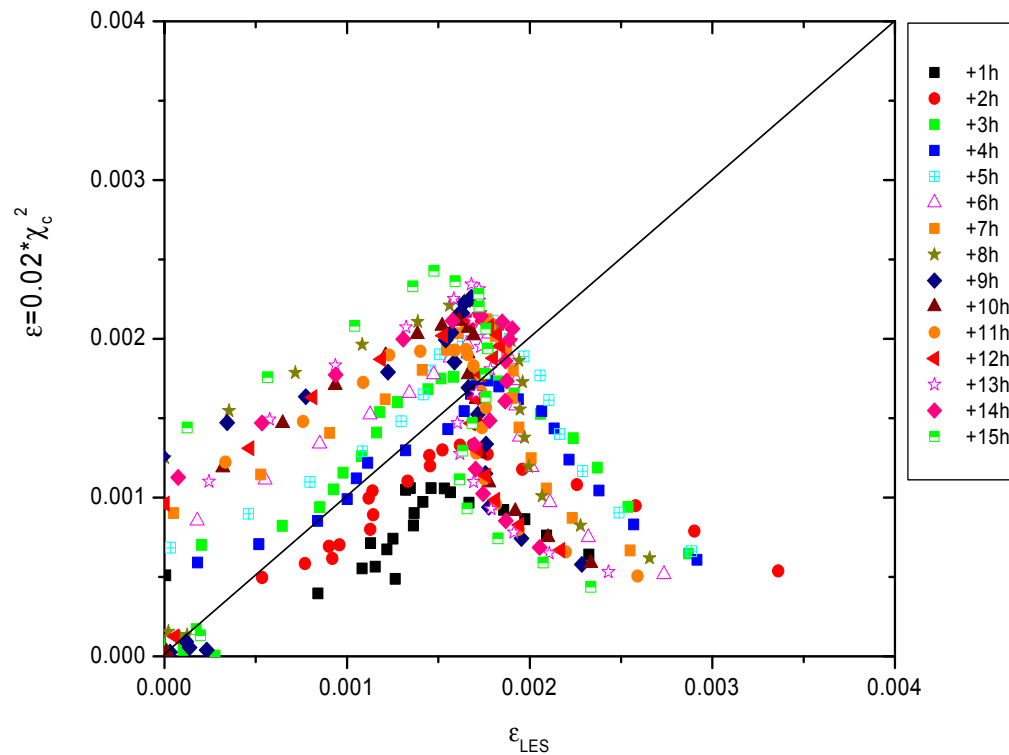
$$\varepsilon_{KF} = \varepsilon_0 \cdot \chi_c^2$$

$$\delta_{KF} = \varepsilon_0 \cdot (1 - \chi_c^2)$$

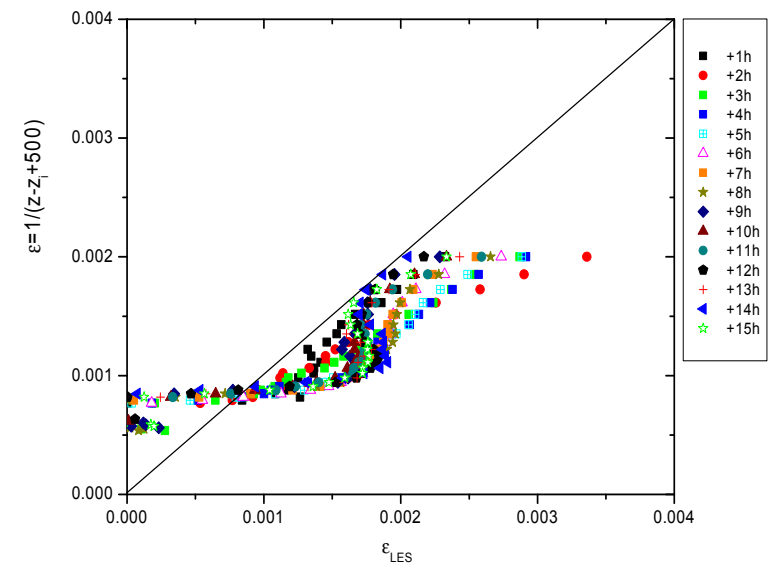
How well do they perform?  
(validated against LES diagnosis)

# Kain Fritsch entrainment (dilution)

BOMEX case: Kain Fritsch  $\varepsilon$  with optimal  $\varepsilon_0$



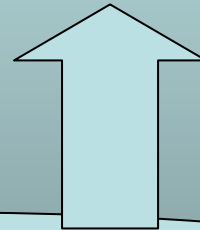
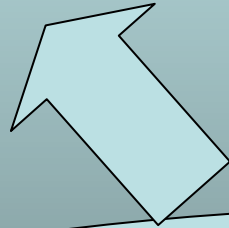
BOMEX case:  $\varepsilon = (z - z_i + 500)^{-1}$



Kain Fritsch  $\varepsilon$  not very suitable for describing the dilution

But there is something else  
how about the mass flux profile?

$$\varepsilon_{KF} = \varepsilon_0 \cdot \chi_c^2 \quad \delta_{KF} = \varepsilon_0 \cdot (1 - \chi_c^2)$$



$\varepsilon_{KF}$  and  $\delta_{KF}$  vary in a similar but opposite way to  $\chi_c^2$  and therefore have a similar influence on mass flux profile variations

# However

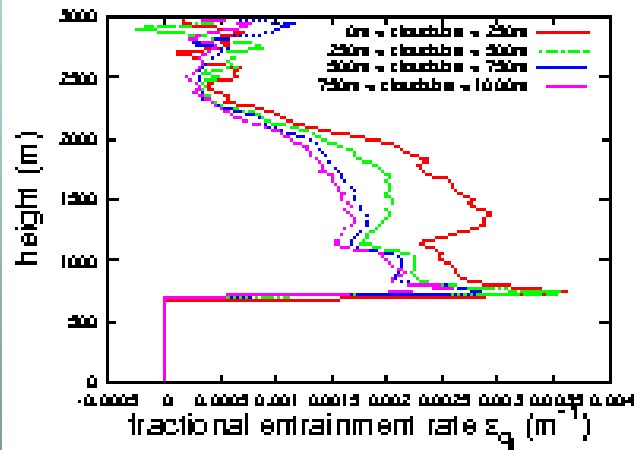
- Variations in the mass flux profile are strongly dominated by  $\delta$ !

- Empirical arguments
- Theoretical arguments

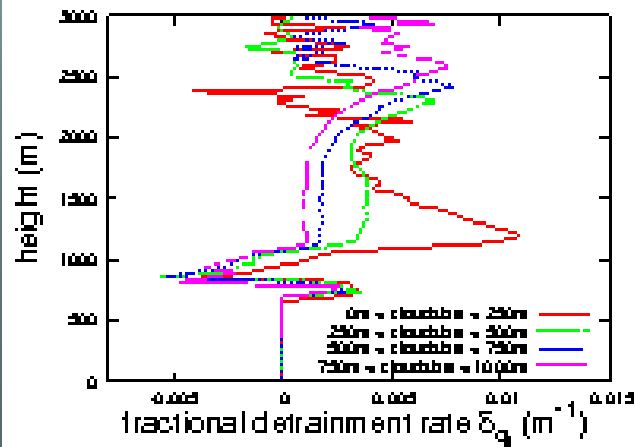
# Empirical arguments

Much larger variation in  $\delta$  from case to case, hour to hour, different cloud sizes

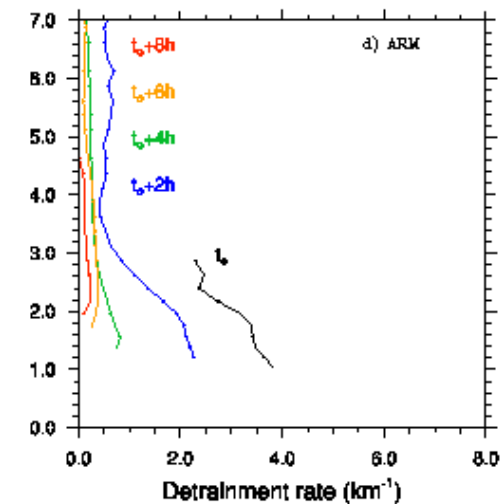
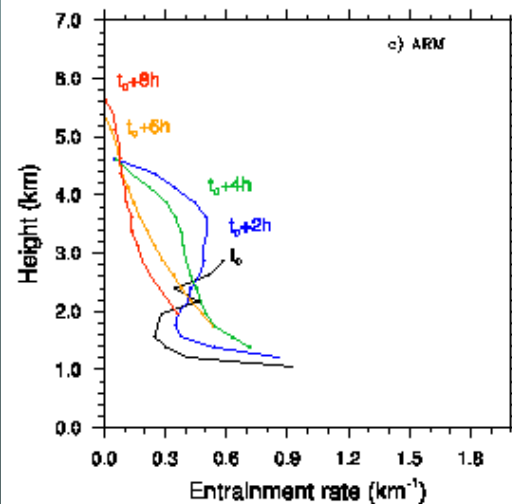
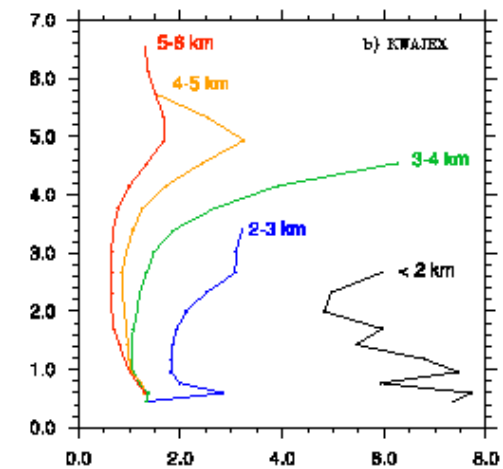
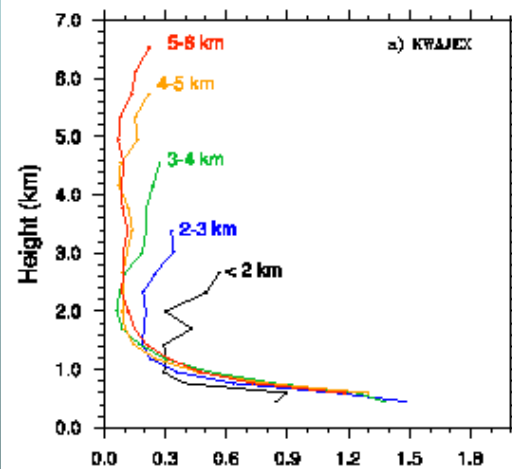
Jonker et al., 2006



(a)

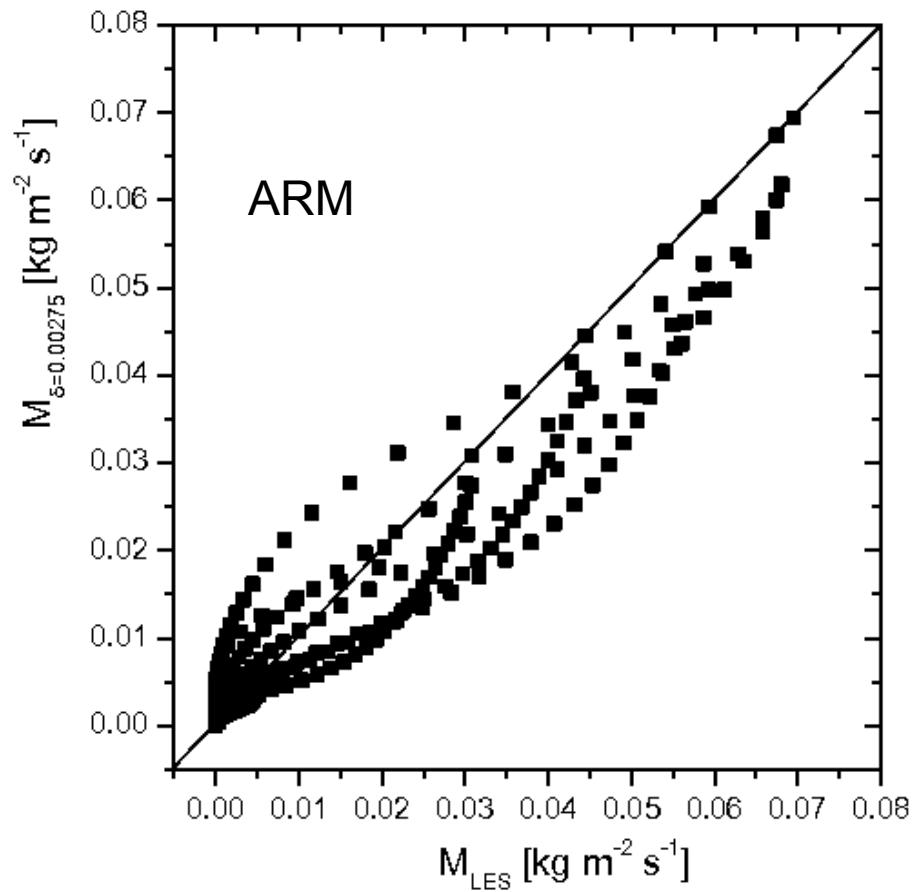


Hohenegger, 2011

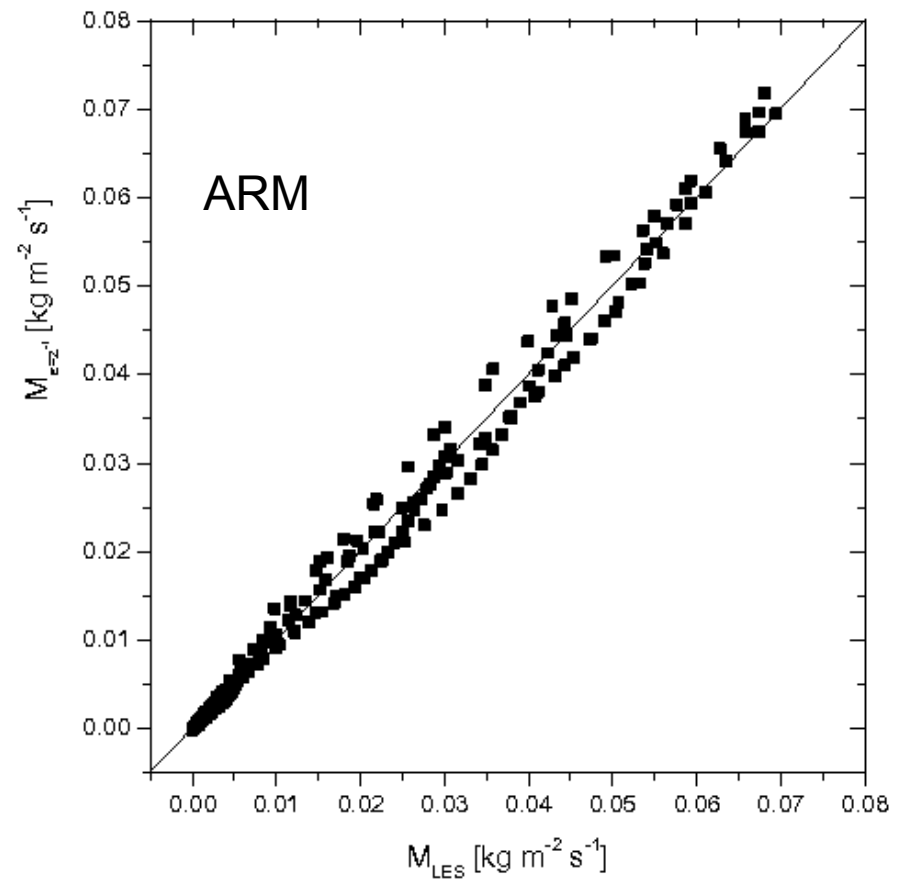


# Empirical arguments

Optimal fixed  $\delta$  and  $\epsilon_{LES}$



Optimal fixed  $\epsilon$  and  $\delta_{LES}$



# Theoretical arguments

*De Rooy & Siebesma, QJRMS 2010*

Starting from general in-cloud field budget equation for  $q_t$  (Siebesma, 1998)

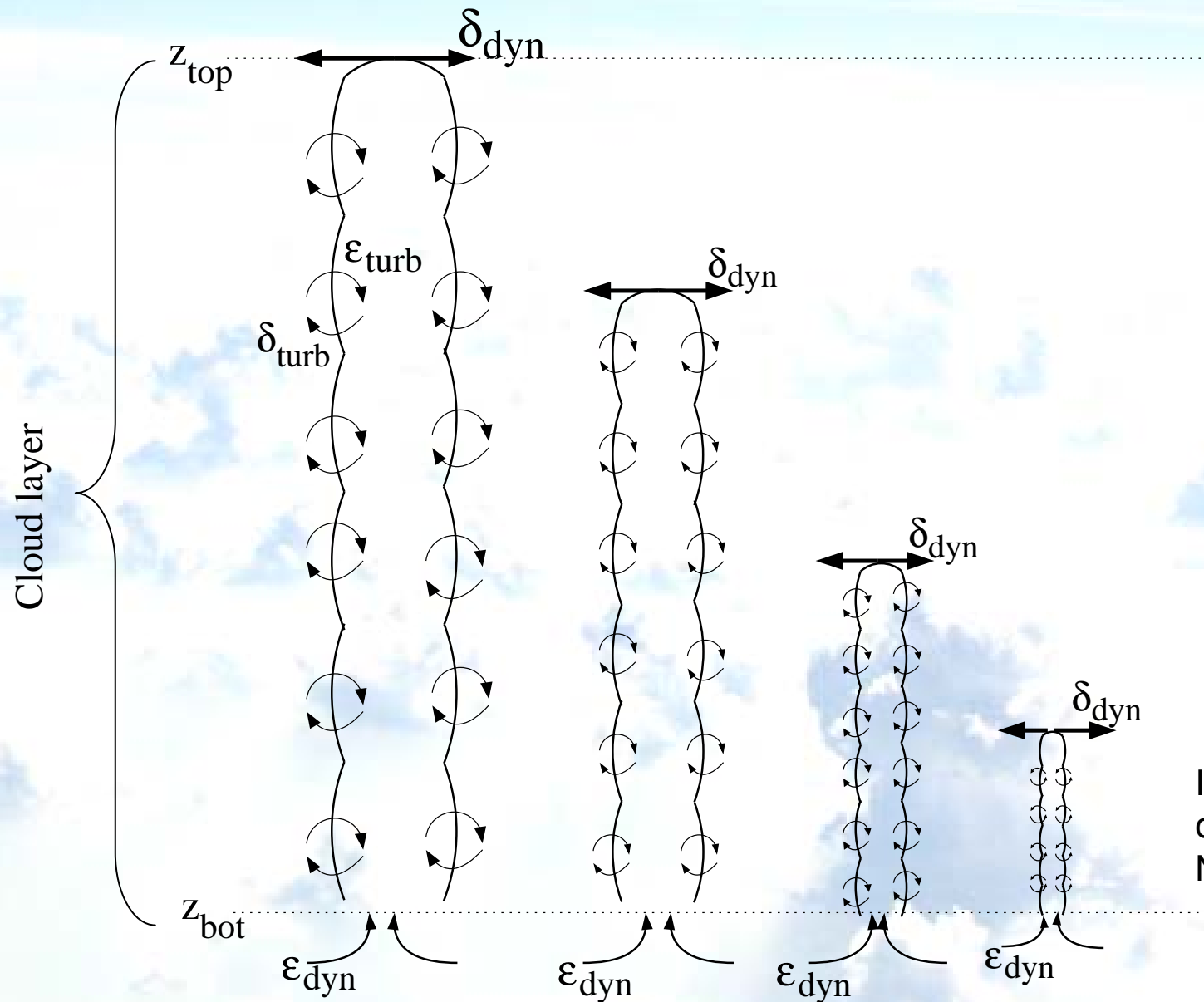
$$\varepsilon = \frac{\eta L_b}{A_c} + H(-u_b) \frac{1}{M} \frac{\partial M}{\partial z} \equiv \varepsilon_{turb} + \cancel{\varepsilon_{dyn}}$$

Shallow Convection:  
Usually  $dM/dz < 0$

$$\delta = \frac{\eta L_b}{A_c} - H(u_b) \frac{1}{M} \frac{\partial M}{\partial z} = \delta_{turb} + \delta_{dyn}$$



# Cloud ensemble (divergent (shallow) condition)

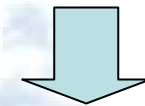


$$\varepsilon = \varepsilon_{turb} + \cancel{\varepsilon_{dyn}}$$

$$\delta = \delta_{turb} + \delta_{dyn}$$

In the cloud layer:

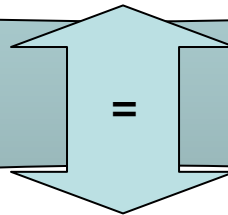
$$\delta \sim \frac{1}{M} \frac{\partial M}{\partial z} \sim \frac{1}{M} \frac{\Delta M}{\Delta z} \sim \frac{1}{\Delta z}$$



Included in:  
de Rooy & Siebesma 08  
Neggers et al. 09

# What are the consequences?

As far as variations in the (non-dim) mass-flux profile concerns:  
Use a (simple) fixed function for  $\varepsilon$  but a flexible  $\delta$



Parameterize the mass-flux profile  
(in terms of environmental and updraft conditions)

**So no explicit  $\varepsilon$  and  $\delta$  for M profile!**

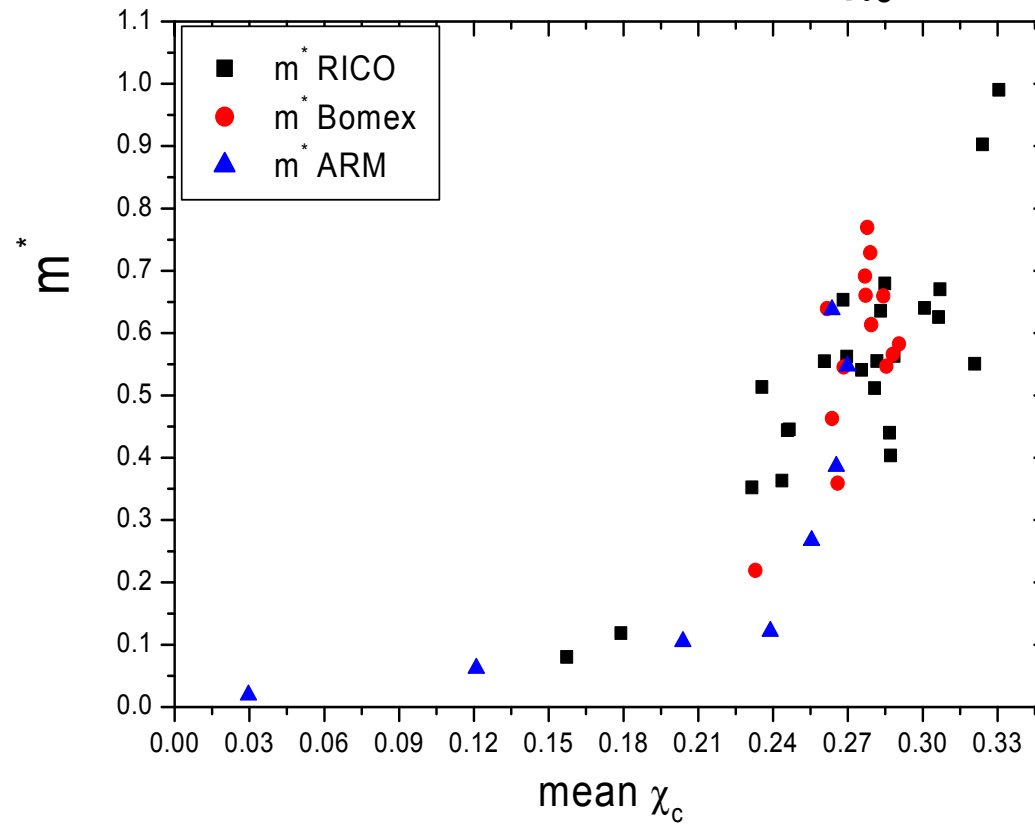


Unconventional:  
Separate entrainment (dilution) and mass flux profile!  
De Rooy & Siebesma 2008  
Neggens et al. 2009

### Some advantages:

- Mass flux parameterizations can be related to observations and LES
- Function of  $\varepsilon$  can be dedicated to a good description of the dilution

From LES, the change of the non-dimensionalized mass flux as a function of  $\overline{\chi_c}$



*De Rooy & Siebesma, 2008*

Short D-tour: How can we proceed with the expressions:

$$\varepsilon = \frac{\eta L_b}{A_c} + H(-u_b) \frac{1}{M} \frac{\partial M}{\partial z} \equiv \varepsilon_{turb} + \varepsilon_{dyn}$$

$$\delta = \frac{\eta L_b}{A_c} - H(u_b) \frac{1}{M} \frac{\partial M}{\partial z} = \delta_{turb} + \delta_{dyn}$$

Use continuity eq. to eliminate  $u_b$

Use vertical velocity eq. to eliminate  $\eta$



Expressions independent of divergence/convergence

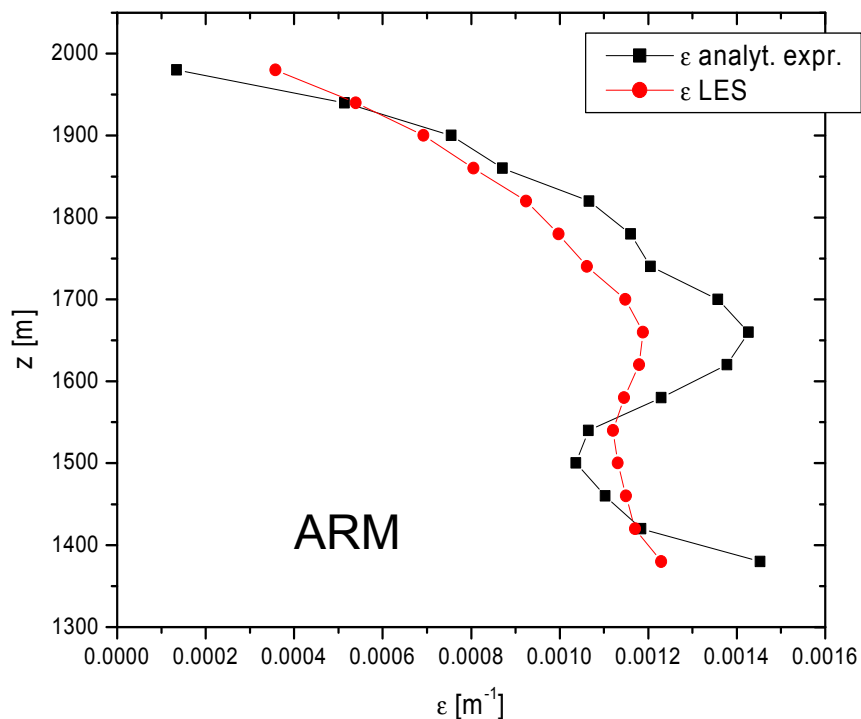
$$\varepsilon_{exp} = \frac{\alpha B}{w_c^2} - \frac{1}{w_c} \frac{\partial w_c}{\partial z}$$

$$\delta_{exp} = \frac{\alpha B}{w_c^2} - \frac{2}{w_c} \frac{\partial w_c}{\partial z} - \frac{1}{a_c} \frac{\partial a_c}{\partial z}$$

!

# How do the analytical expressions perform against LES?

Example for  $\mathcal{E}_{\text{exp}} = \frac{\alpha B}{w_c^2} - \frac{1}{w_c} \frac{\partial w_c}{\partial z}$



Analytical expression cannot be directly applied as parameterization

However, iteration procedure  
Alison Stirling & R. Wong  
(to be submitted to QJRMS)  
Expressions perform well for  
a wide variety of conv. cases

# Conclusions/Recommendations

- Keep parameterizations as simple as possible. Just enough complexity to include the most relevant processes
- Proposed  $\varepsilon$ ,  $\delta$  are strongly coupled to LES (i.o. tuned)
- Treat dilution ( $\varepsilon$ ) and mass-flux profile separately
  - Empirical/physical bases
  - Flexibility
  - Robustness
- Analytical expressions give insight. Also:  $\varepsilon_{\text{exp}}$  promising as parameterization of dilution

An aerial photograph of a tropical atoll, showing a series of white sand beaches and turquoise lagoons separated by shallow reefs. The water transitions from light turquoise near the shore to a deeper blue further out. The sky is filled with numerous white, fluffy clouds. Overlaid on the center of the image is the text "Thank you Questions?" in a bold, yellow, sans-serif font with a black outline.

**Thank you  
Questions?**