

Representation of Cloud Processes in Large Scale Models

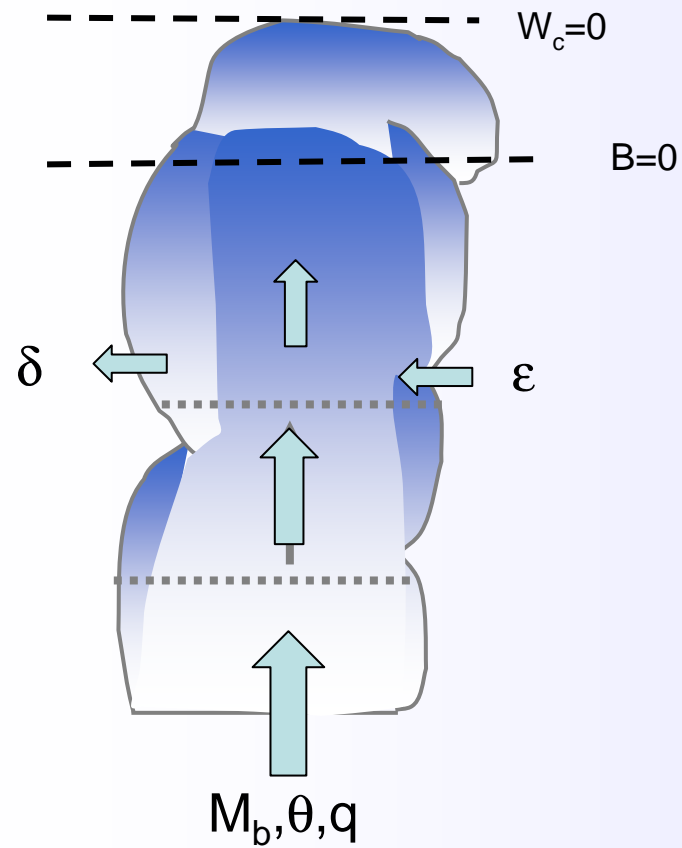
Lecture 3

Cloud Parameterizations

Outlook

A. Pier Siebesma

All nice and fine, but.....



We need to know:

1. What is the entrainment and detrainment
2. **At which height does the cloud stop (wc-equation)**
3. What are the values of M, θ, q at cloud base (Closure)
4. When does convection initiate (triggering)

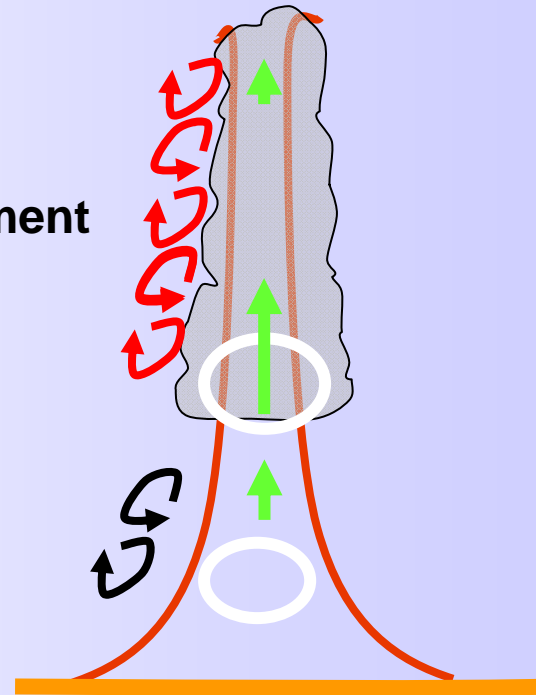
1.

Vertical Velocity In Cumulus Convection

Why?

- Overshoot
- Triggering
- Mass Flux $M \sim w_c \sigma$
- not all CMIP5 models use wc-eq

Entrainment



$$w_u \frac{\partial w_u}{\partial z} = -b \epsilon w_u^2 + aB$$

Vertical velocity

This equation can be derived from the updraft equation where it is assumed that the pressure gradient term is absorbed in a “reduction” factor of the buoyancy.

A wide range of realisations

$$w_u \frac{\partial w_u}{\partial z} = -b \varepsilon w_u^2 + aB$$

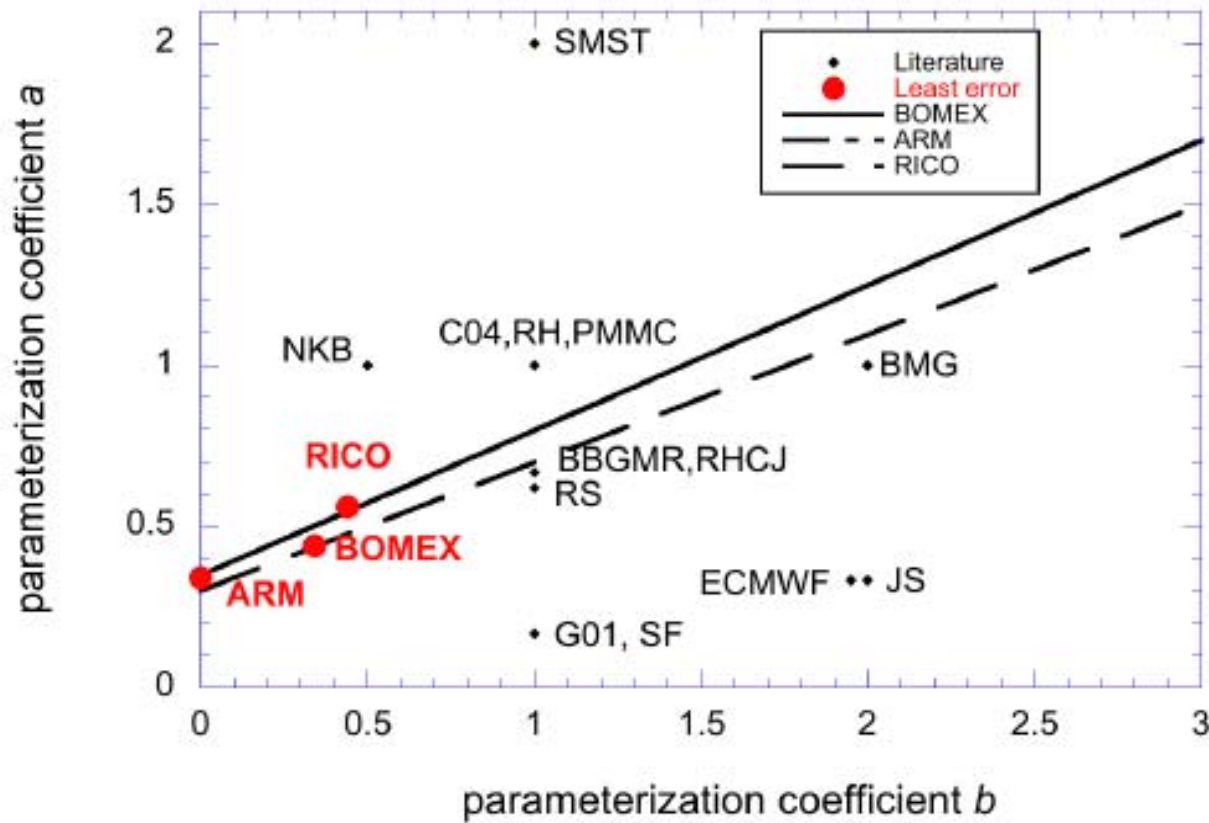
Reference	Acronym	Eq.	a	b	Remarks
Simpson and Wiggert (1969)		(1)	$\frac{2}{3}$		$\frac{1}{2} \frac{\partial w_u^2}{\partial z} = aB_c - 0.18 \frac{w_u^2}{R}$, R is cloud radius
Bechtold et al. (2001)	BBGMR	(12)	$\frac{2}{3}$	1	
Gregory (2001)	G01	(11)	$\frac{1}{6}$	1	$\frac{1}{2} \frac{\partial w_u^2}{\partial z} = aB_c - (b\delta + bc)w_c^2$, $b' = \frac{1}{2}$
Von Salzen and McFarlane (2002)	SF	(29)	$\frac{1}{6}$	1	
Jakob and Siebesma (2003)	JS	(7)	$\frac{1}{3}$	2	
Bretherton et al. (2004)	BMG	(17)	1	2	
Cheinet (2004)	C04	(1)	1	1	
Soares et al. (2004)	SMST	(6)	2	1	
Rio and Hourdin (2008)	RH	(5)	1	1	$\frac{\partial \sigma w_u^2}{\partial z} = a\sigma B_c - b'\delta\sigma w_c^2$, $b' = \frac{1}{2}$ b value found after substitution of Eq. (4)
Neggens et al. (2009)	NKB	(12)	1	$\frac{1}{2}$	$\frac{1}{2}(1 - 2\mu) \frac{\partial w_u^2}{\partial z} = aB_c - bcw_c^2$, $\mu = 0.15$
Pergaud et al. (2009)	PMMC	(7)	1	1	
Rio et al. (2010)	RHCJ	(9)	$\frac{2}{3}$	1	$\frac{1}{2} \frac{\partial w_u^2}{\partial z} = aB_c - (b' + bc)w_c^2$, $b' = 0.002$
De Rooy and Siebesma (2010)	RS	(27)	0.62	1	
ECMWF c36r1 (2010)	ECMWF	(6.9)	$\frac{1}{3}$	1.95	
Kim and Kang (2011)	KK	(11)	$\frac{1}{6}$	2	$\frac{1}{2} \frac{\partial w_u^2}{\partial z} = a(1 - C_\epsilon b)B_c$, $C_\epsilon = 1/\overline{RH} - 1$

Which one to use?

De Roode et al 2012

optimal parameters a and b estimated from LES simulations

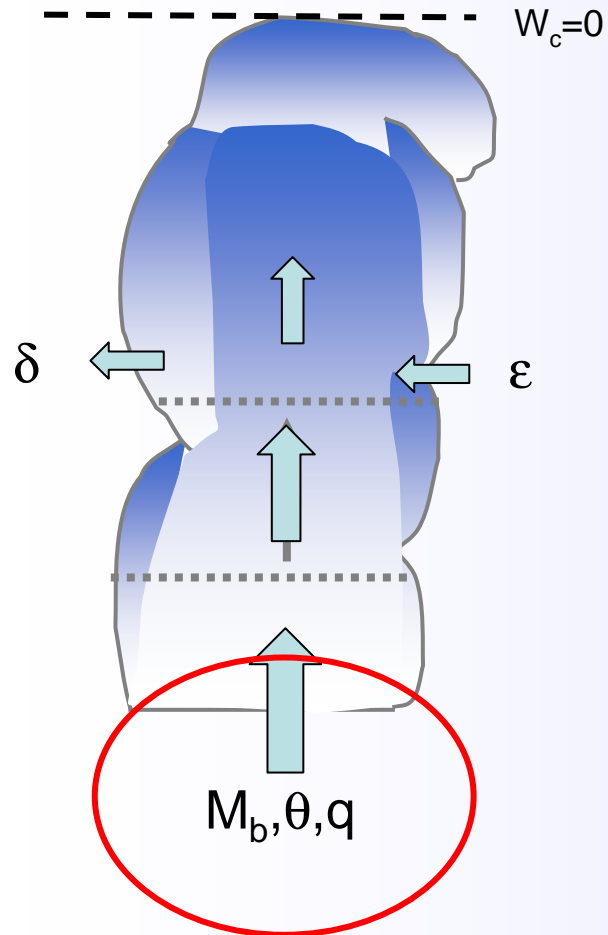
$$w_u \frac{\partial w_u}{\partial z} = -b \epsilon w_u^2 + aB$$



$$w_u \frac{\partial w_u}{\partial z} = \frac{1}{3} B$$

Only 30% of buoyancy is effectively used for transformation to organized vertical velocity.

All nice and fine, but.....



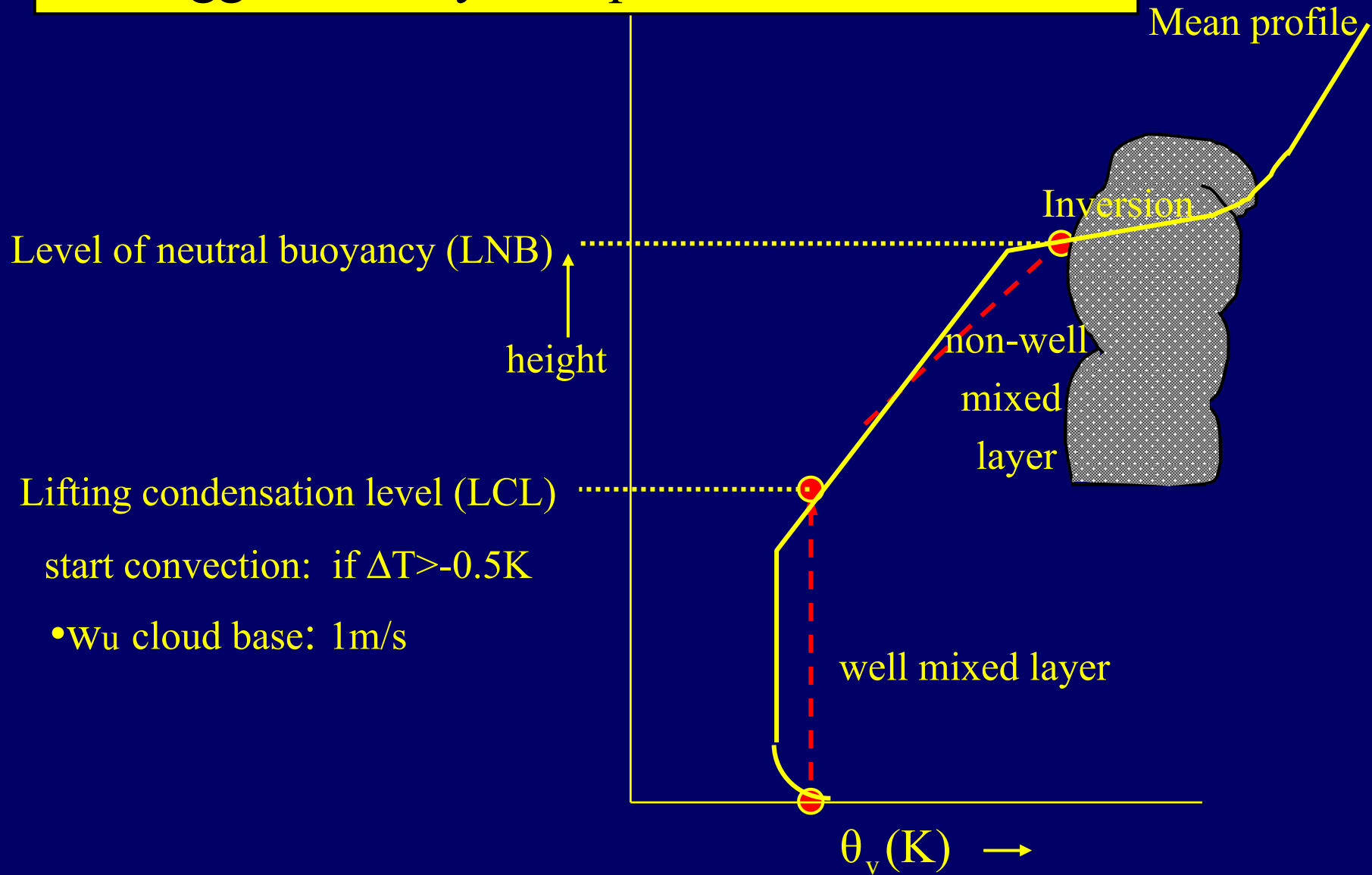
We need to know:

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2.

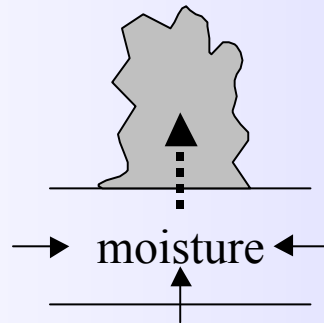
Closure

Trigger: usually : simple adiabatic ascent



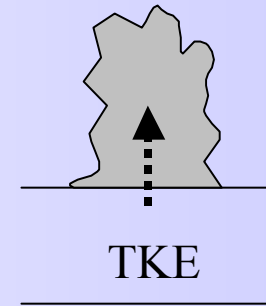
Coupling of M_b to
sub-cloud layer

(Tiedtke 1989)



$$M_b^c (q_t^c - \bar{q}_t)_b = \overline{w'q'^s} + \text{horizontal advection}$$

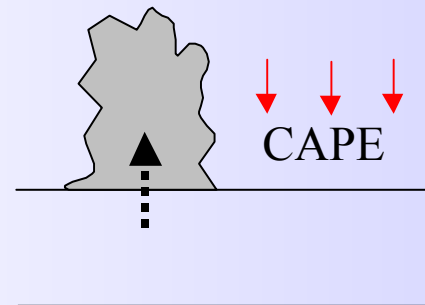
(Grant 1999)



$$M_b^c = 0.03 w_{sub}^*$$

Coupling of M_b to
cloud layer

Fritsch & Chappell (1980)



- The closure gives the M_b needed to break down the given amount of CAPE during time t by compensating subsidence.

3.

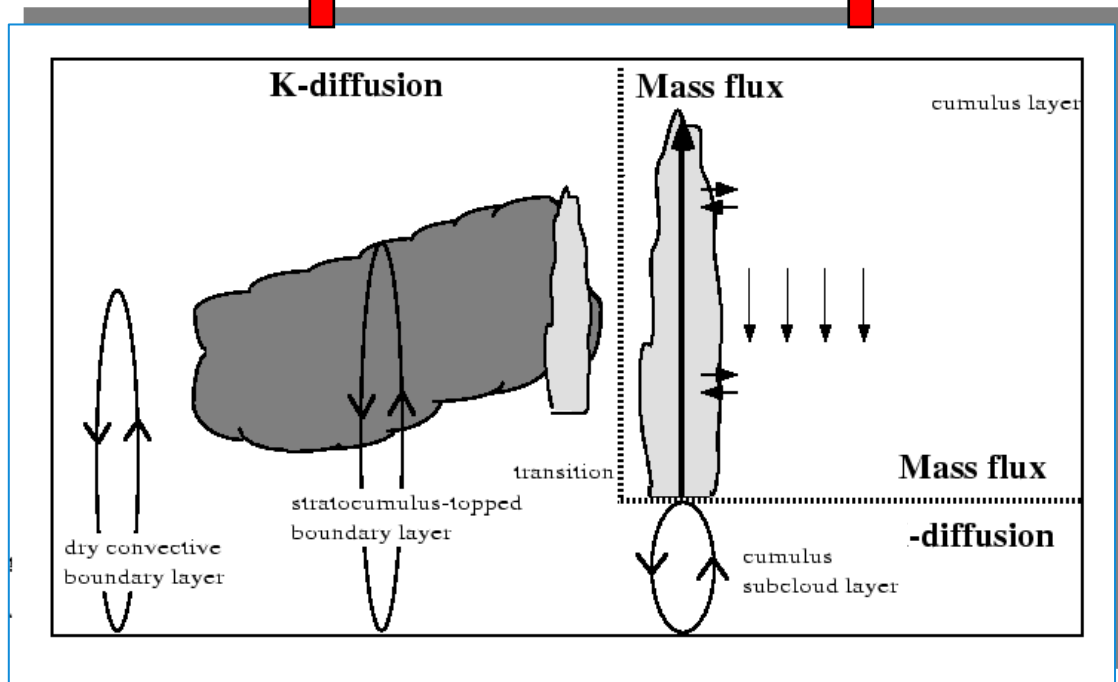
Coupling Transport Schemes

Wrap up

$$\overline{w'\phi'} \cong -K \frac{\partial \bar{\phi}}{\partial z}$$

$$\overline{w'\phi'} \cong M(\phi_u - \bar{\phi})$$

$$\frac{\partial \bar{\phi}}{\partial t} \cong -\frac{\partial}{\partial z} (\overline{w'\phi'}) + \bar{S}$$

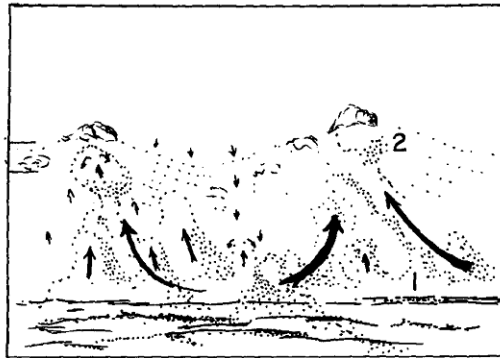


Problems with transitions between different regimes:

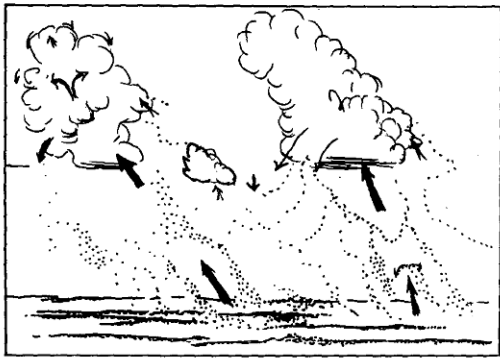
dry pbl → shallow cu

scu → shallow cu

shallow cu → deep cu



(a)

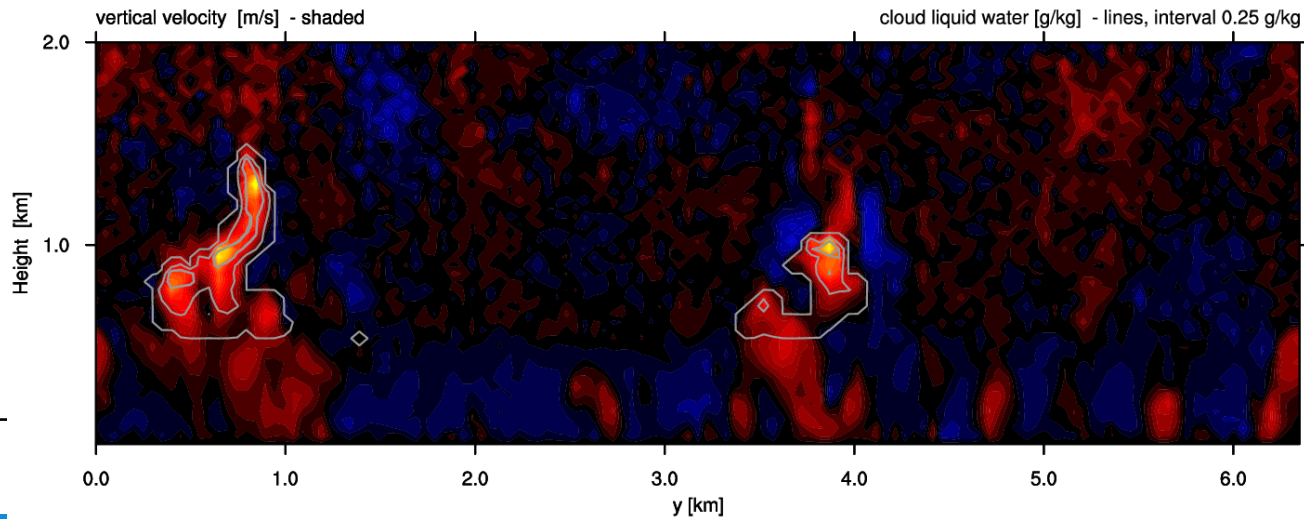


(b)

- LeMone & Pennell (1976, MWR)

Cumulus clouds are the condensed, visible parts of updrafts that are deeply rooted in the subcloud mixed layer (ML)

LES BOMEX vertical cross-section

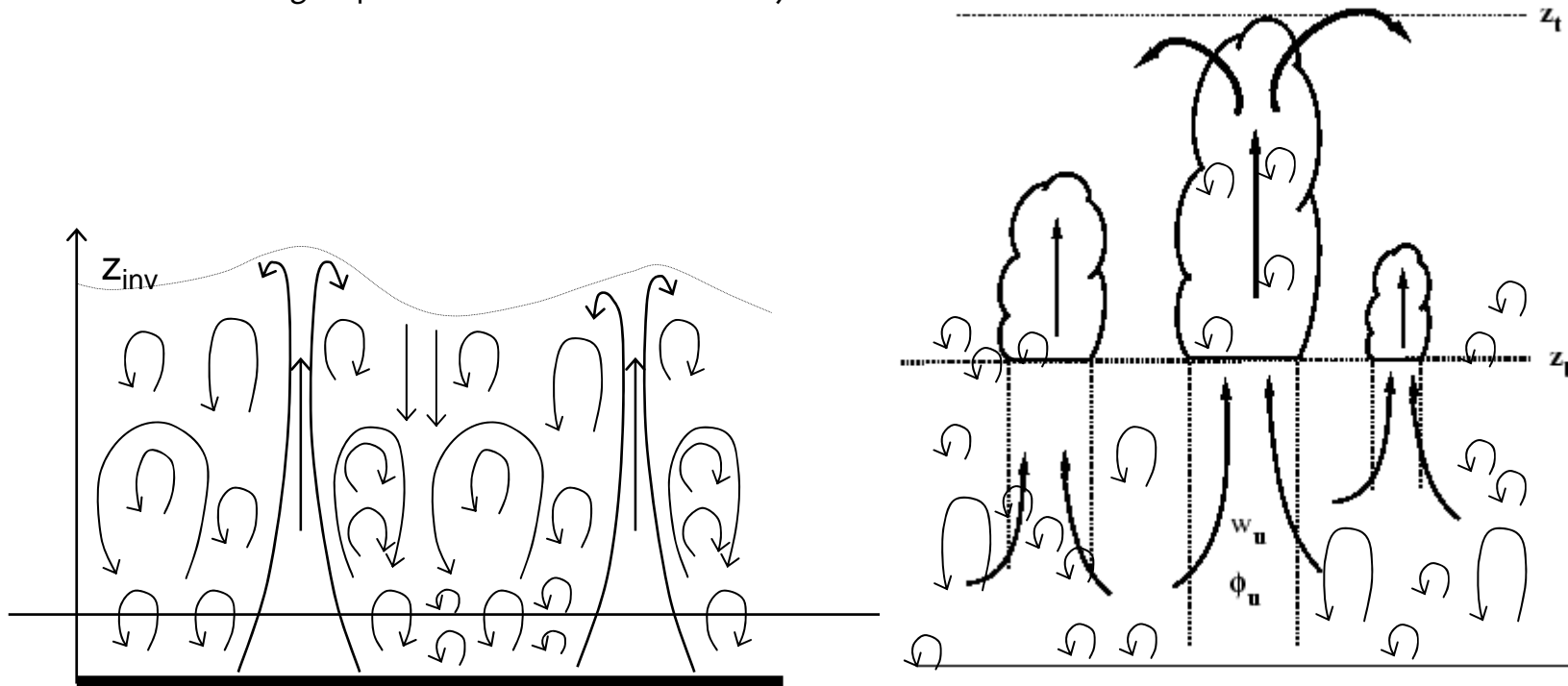


Eddy-Diffusivity/Mass Flux (EDMF) approach

- Nonlocal (Skewed) transport through strong updrafts in clear and cloudy boundary layer by advective Mass Flux (MF) approach.
- Remaining (Gaussian) transport done by an Eddy Diffusivity (ED) approach.

Advantages :

- One updraft model for : dry convective BL, subcloud layer, cloud layer.
- No trigger function and cloud base height closure for moist convection needed
- No switching required between moist and dry convection needed



The (simplest) Mathematical Parameterization Framework :

$$\overline{w' \phi'} = \sigma_u \overline{w' \phi'^u} + (1 - \sigma_u) \overline{w' \phi'^e} + \sigma_u w_u (\phi_u - \bar{\phi})$$

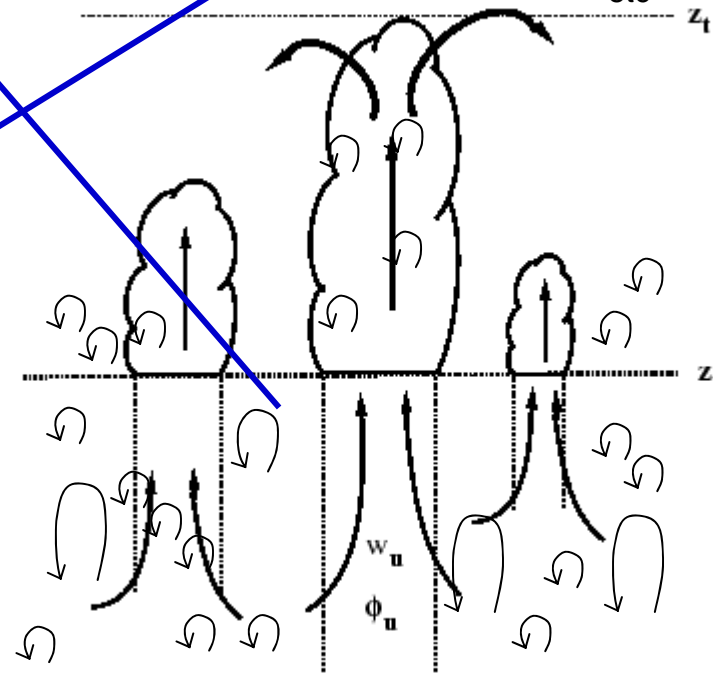
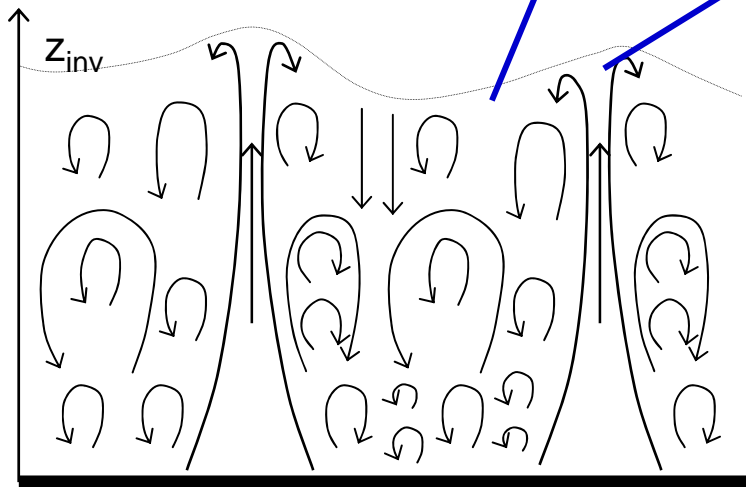
$$\cong -K \frac{\partial \bar{\phi}}{\partial z} + M (\phi_u - \bar{\phi})$$

siebesma&teixeira 2000

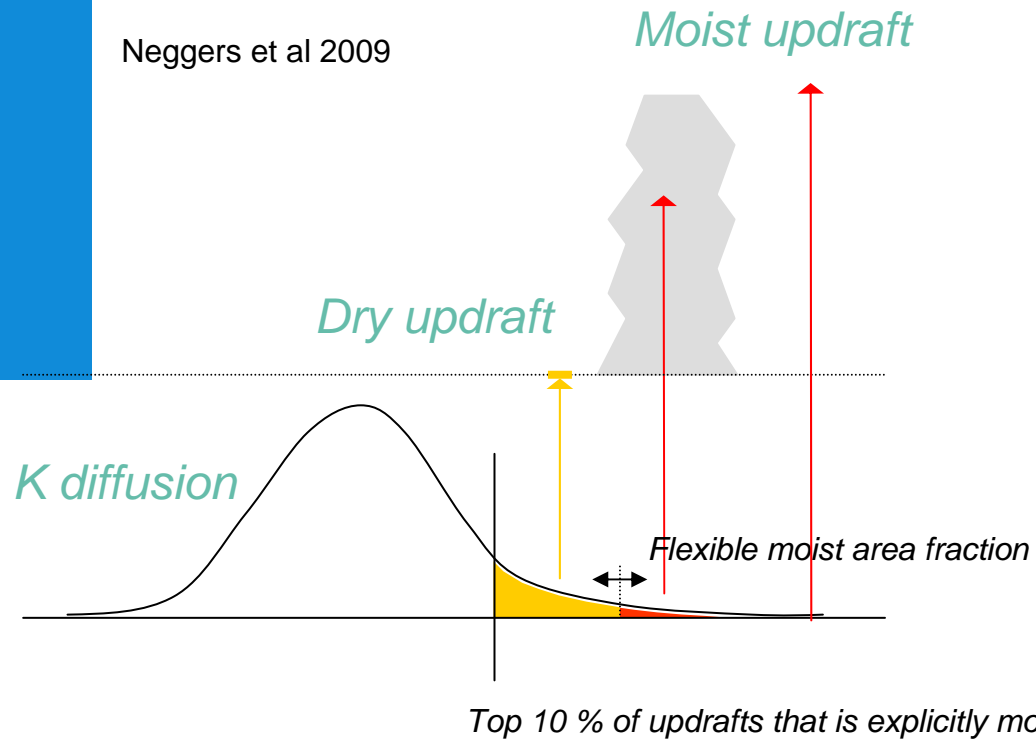
Hourdin et al 2002

Pergaud 2006

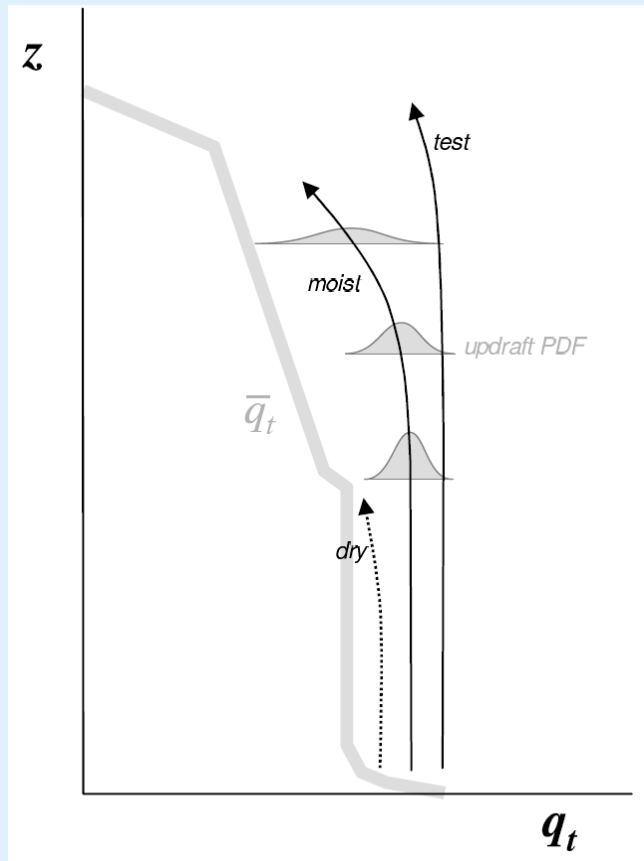
etc



Neggers et al 2009



$$\overline{w'\phi'}_{PBL} = -K \frac{\partial \bar{\phi}}{\partial z} + \sum_{i=1}^N M_i (\phi_i - \bar{\phi})$$



•Assume a Gaussian joint PDF(θ_l, q_t, w) shape for the cloudy updraft.

•Mean and width determined by the multiple updrafts

•Determine everything consistently from this joint PDF

$$a_u, w_u, \theta_{l,u}, q_{t,u}$$

An reconstruct the flux:

$$\overline{w' \psi'} = a_u w_u (\psi_u - \bar{\psi})$$

Remarks:

- No closure at cloud base
- No detrainment parameterization

~~$$\frac{1}{M} \frac{\partial M}{\partial z} = \epsilon - \delta$$~~

4.

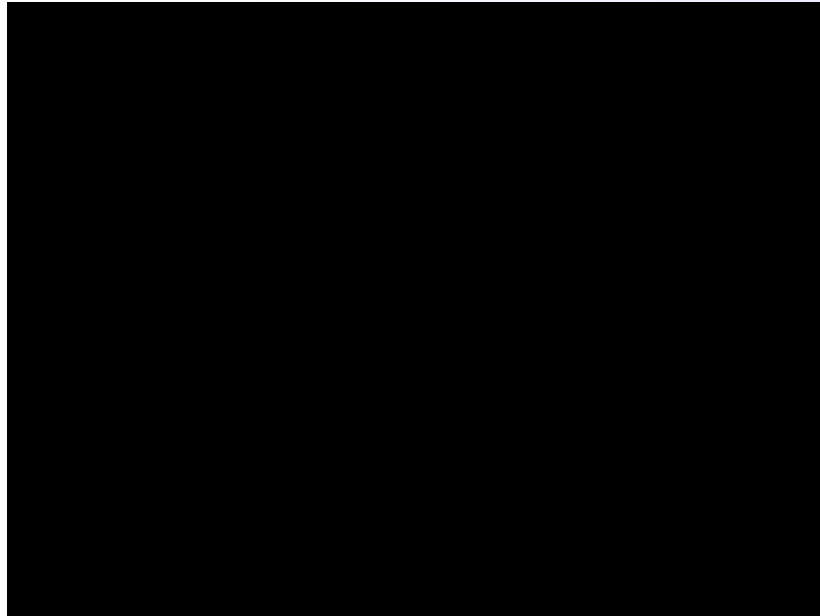
Cloud Schemes

Why do we need a cloud scheme?

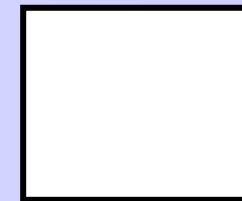
Why do we need a cloud scheme?

- Cloud radiative effects
 - cloud fraction
 - cloud condensate (cloud water and ice)
- Latent Heat Effects (condensation/evaporation effects, precipitation)
 - These effects are usually referred to as “large scale” (i.e. large scale precipitation) the other contribution residing from the convection schemes (convective precipitation). The distinction is rather arbitrary and depend on the model design, resolution etc.....)

How do we build such a scheme?



$$\Delta y \approx 50m$$



$$\Delta x \approx 50m$$

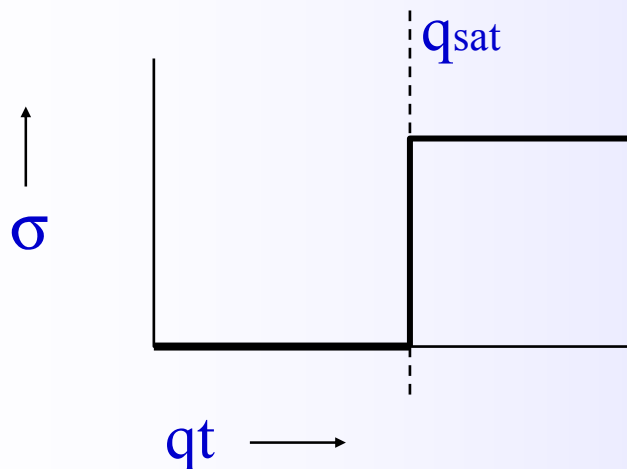
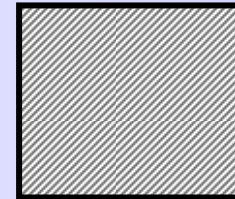
Cloud Schemes in LES

- Simple: All or Nothing:

$$\begin{cases} \sigma_c = 0, \\ q_c = 0, \end{cases} \quad \text{if } \bar{q}_t - \bar{q}_{sl} < 0$$



$$\begin{cases} \sigma_c = 1, \\ q_l = \alpha(q_t - q_{sl}), \end{cases} \quad \text{if } q_t - q_{sl} > 0$$



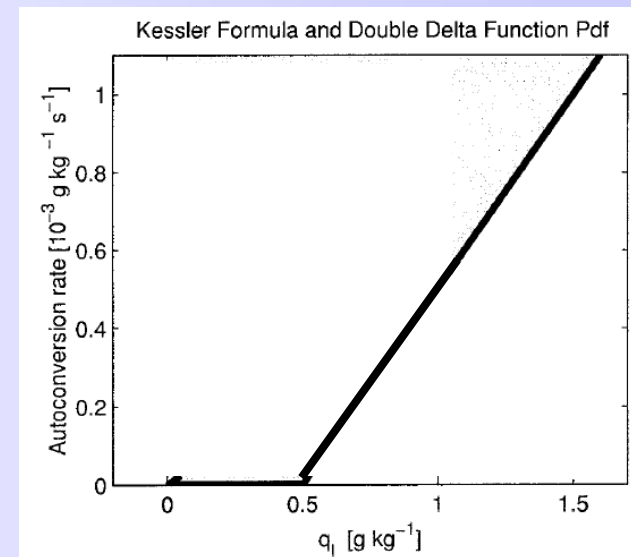
Cloud adjustment

Autoconversion (transition from cloud water to rain)

$$\left(\frac{\partial q_r}{\partial t} \right)_{au} = G_p$$

Autoconversion (Kessler, 1969)

$$G_p = \begin{cases} k_0 (q_c - q_{c,crit}) & \text{if } q_l > q_{l,crit} \\ 0 & \text{otherwise} \end{cases}$$



Many different formulations (including dependencies on cloud droplet number density)

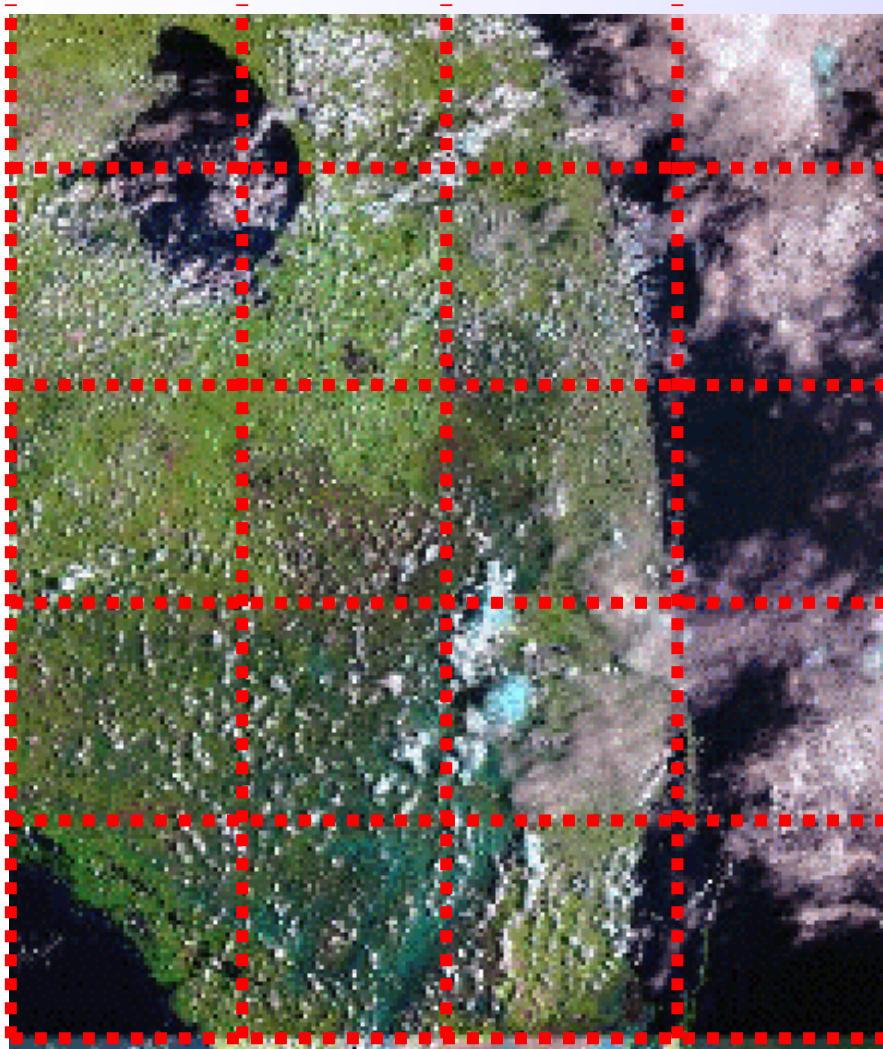
Autoconversion:	q_c	N_c	T	
	1		H	Kessler (1969)
	1		exp	Sundqvist (1978)
	2.47	-1.79		Khairoutdinov and Kogan (2000)
	4.7	-3.3		Beheng (1994)
	4	-2		Seifert and Beheng (2001)
	2.33	-0.33	H	Tripoli and Cotton (2000)
	2.33	-0.33	H	Liu and Daum (2006)
	2.74	-1.35		.

$$\left(\frac{\partial q_r}{\partial t}\right)_{auto} = k_0 q_c^a N_c^{-b} T$$

\uparrow
 $N_{aerosol}$

Specific choice of the autoconversion is often used to calibrate the TOA global energy budget

But does this work for coarser resolutions?

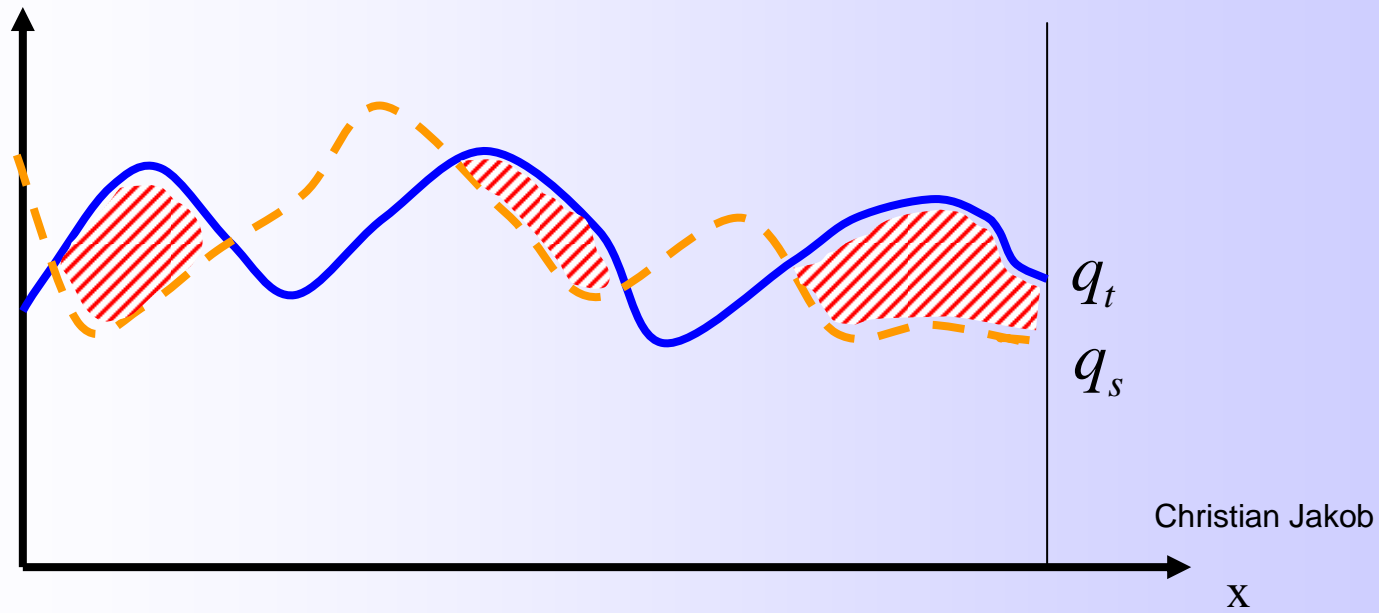


50 km

$\Delta y \approx 50km$

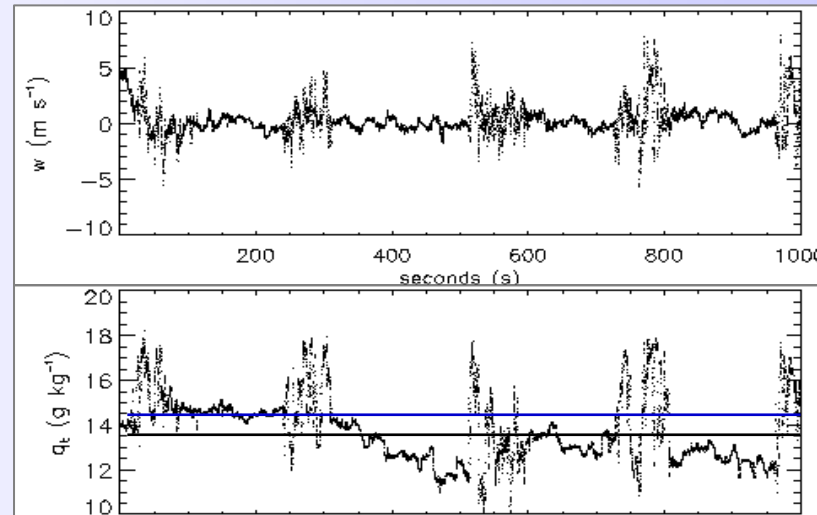
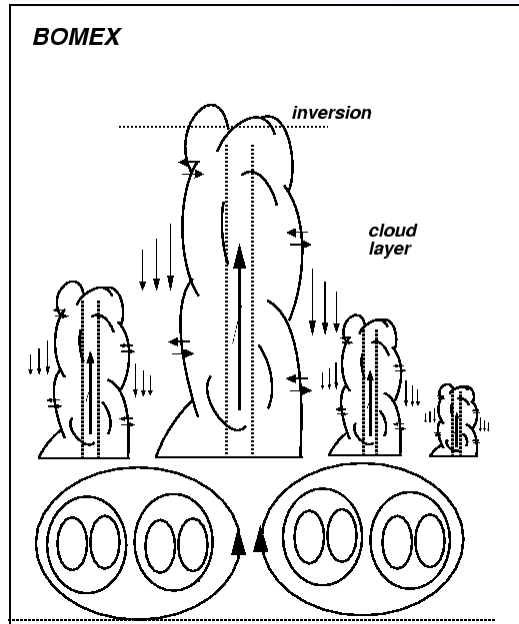


$\Delta x \approx 50km$

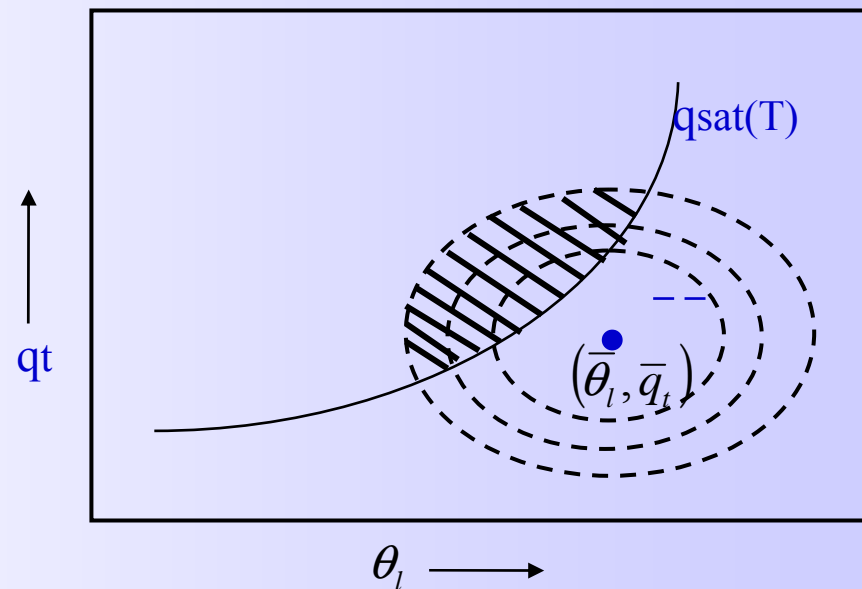


- Due to subgrid variability of humidity and temperature only parts of the grid box are oversaturated (and hence cloudy).
- So we can have clouds in a gridbox even if the mean RH in the gridbox < 1 .

So.... “All or Nothing” does not work if the resolution does not resolve clouds!!!!



Joint Probability
Distribution of θ_l and q_t



Let's assume we know this Joint pdf

$$a_c = \iint H(q_t - q_s) P(\theta_\ell, q_t) dq_t d\theta_\ell \quad (3)$$

$$q_l = \iint (q_t - q_s) H(q_t - q_s) P(\theta_\ell, q_t) dq_t d\theta_\ell$$

$$\text{with } H(x) = \begin{cases} 0, & x < 0 \\ 1, & x > 0 \end{cases}$$

Convenient to introduce:

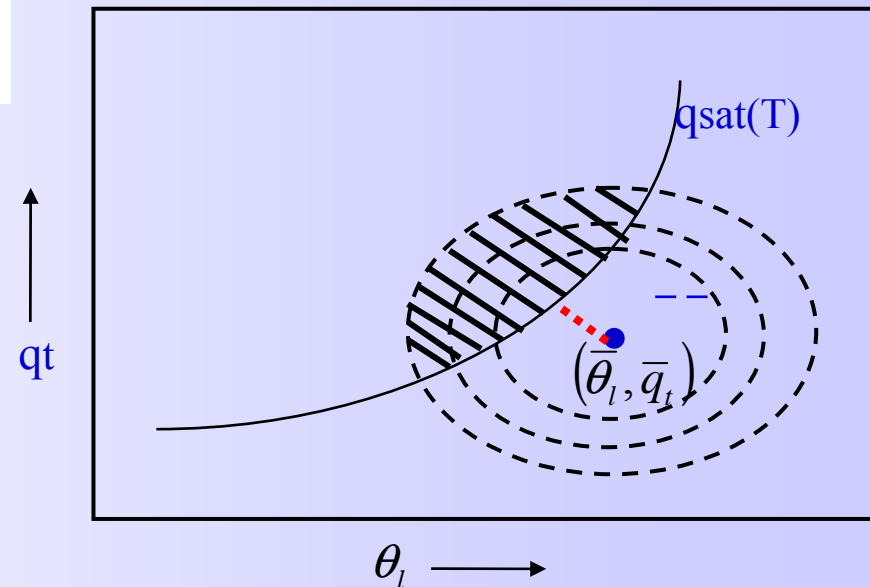
"The distance to the saturation curve"

$$s = q_t - q_s(p, T)$$

Normalise s by its variance

$$t \equiv s/\sigma_s$$

$$\sigma_s^2 = \overline{s'^2} = a^2 \overline{q_t'^2} - 2ab \overline{q_t' \theta_\ell'} + b^2 \overline{\theta_\ell'^2}$$



so that a and q_ℓ can be written in single variable PDF

$$\begin{aligned} a_c &= \int_0^\infty G(t) dt \\ \bar{q}_\ell / \sigma_s &= \int_0^{+\infty} t G(t) dt \end{aligned} \tag{9}$$

What to choose for $G(t)$??

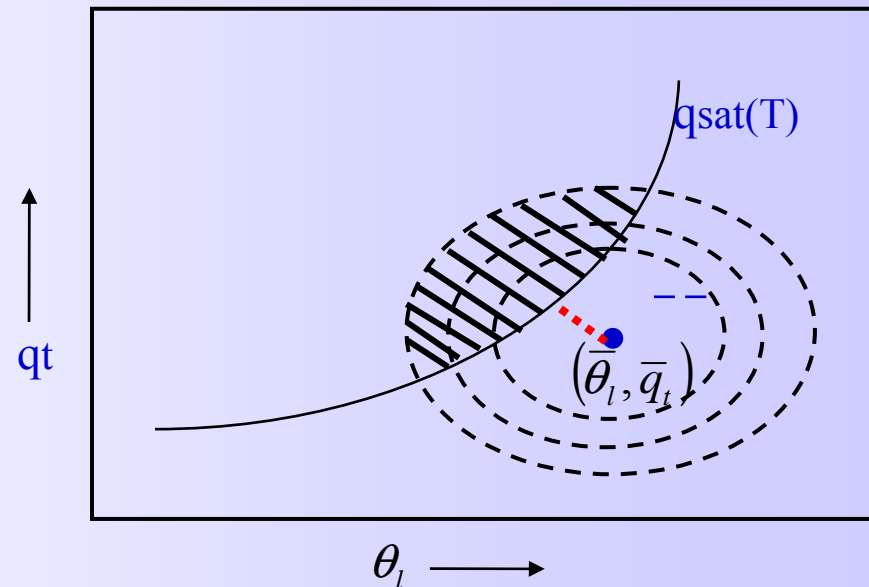
so that a and q_ℓ can be written in single variable PDF

$$\begin{aligned} a_c &= \int_0^\infty G(t) dt \\ \bar{q}_\ell / \sigma_s &= \int_0^\infty t G(t) dt \end{aligned} \quad (9)$$

What to choose for $G(t)$??

The Gaussian Case

$$G(t) dt = \frac{1}{\sqrt{(2\pi)}} \exp(-t^2/(2)) dt \quad (10)$$



$$a_c = \frac{1}{2} \left(1 + \operatorname{erf}(\bar{t} / \sqrt{2}) \right)$$

$$\frac{\bar{q}_c}{\sigma_s} = \alpha \bar{t} + \sqrt{\frac{1}{2\pi}} \exp(\bar{t}^2 / 2)$$

$$Q \equiv \bar{t} = (\bar{q}_t - \bar{q}_s) / \sigma_s$$

So if we know the variance of s (or the variance of q_t and θ_l and its covariance) we know the cloud fraction and the condensed water content.

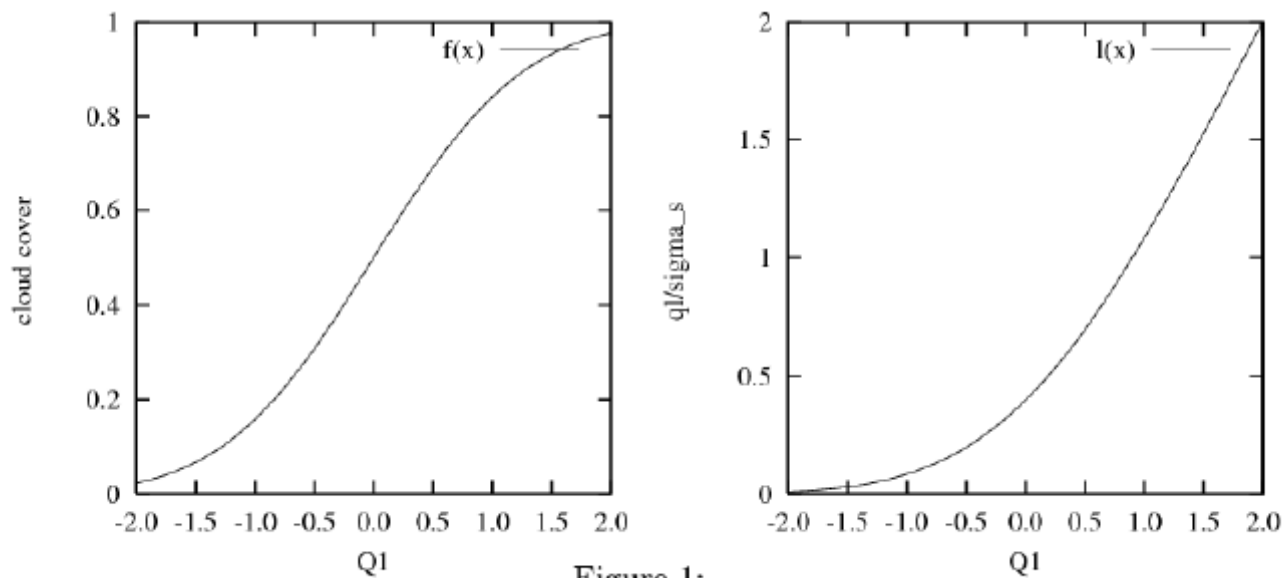
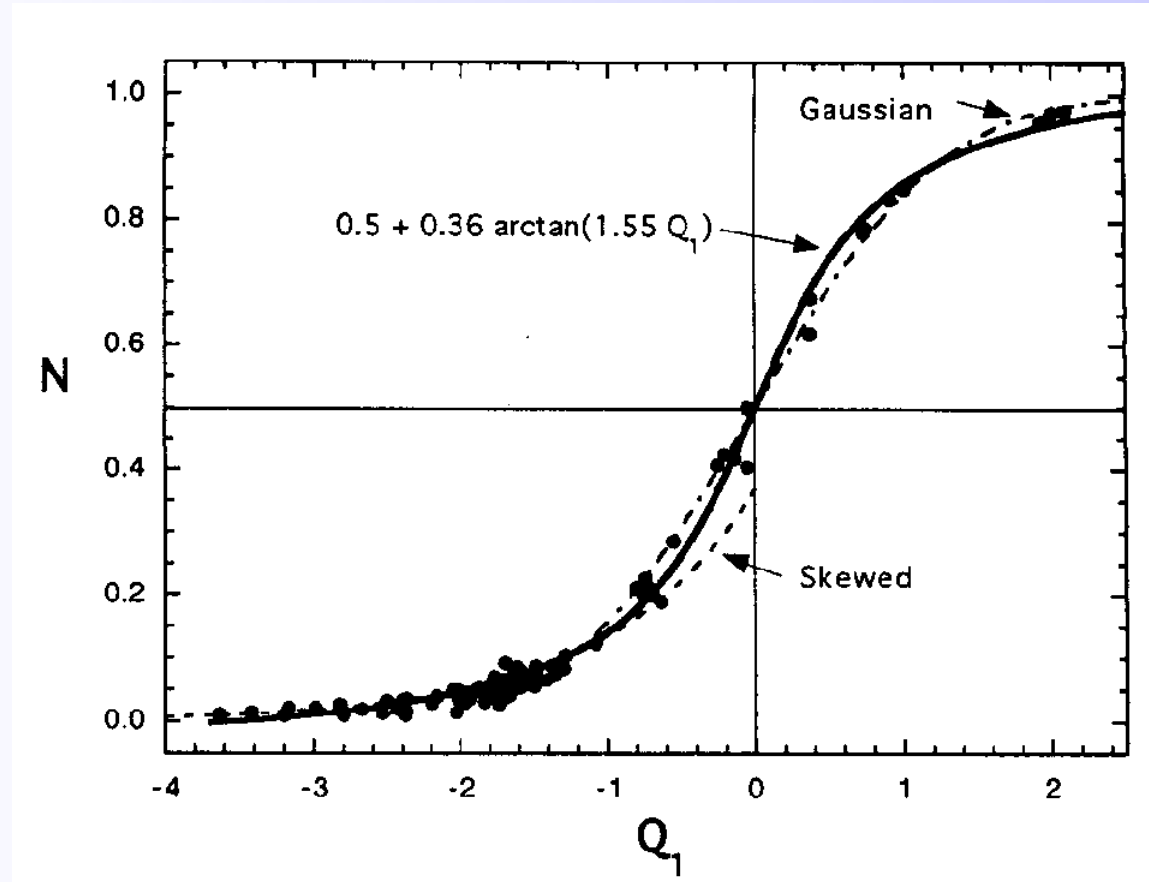


Figure 1:

Evaluation (with LES) (bl-clouds)

↑
Cloud cover

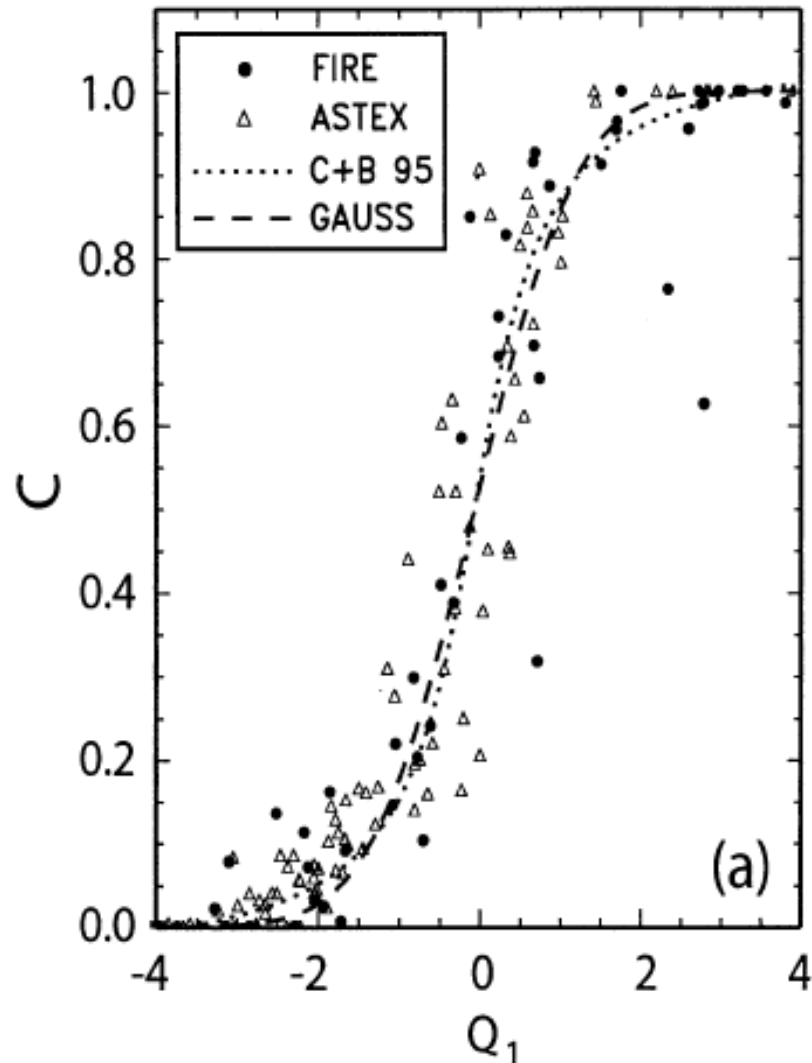


Bechtold and Cuijpers JAS 1995

Bechtold and Siebesma JAS 1999

$$Q \equiv \bar{t} \equiv \frac{\bar{q}_t - \bar{q}_s}{\sigma_s}$$

Evaluation (with obs) (bl-clouds)



(Wood et al 2000)

Remarks:

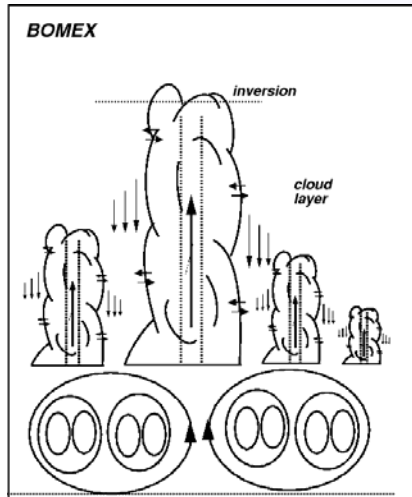
1. Gaussian PDF “surprisingly good” but many more complicated pdf’s have been proposed (Lewellen and Yoy 1993, Tompkins 2002, Neggers et al 2007, poster Mathias etc etc)
2. Correct limit: if $dx \Rightarrow 0$ then $\sigma_s \Rightarrow 0$ and the scheme converges to the all-or-nothing limit
3. Parameterization problem reduced to finding the subgrid variability, i.e. finding σ_s
4. For $Q < -2$ there is essentially zero cloud fraction .

$$RH_{threshold} = 1 - 2 \frac{\sigma_s}{q_s}$$

This makes RH-based cloud schemes essentially pdf-based schemes that assume a constant variance

Where does the variance of s originate from?

Where does the variance of s originate from?



**Convection and
turbulence
parameterization
should give estimate
of σ_s**



$$a_c = f\left(\frac{\bar{q}_t - \bar{q}_s}{\sigma_s}\right)$$
$$q_l = g\left(\frac{\bar{q}_t - \bar{q}_s}{\sigma_s}\right)$$

Cloud scheme :

Connecting Schemes

Variance equation:

$$\frac{\partial \overline{q_t'^2}}{\partial t} = \underbrace{-2\overline{w'q_t'}}_{\text{production}} \frac{\partial \overline{q_t}}{\partial z} - \underbrace{\frac{\partial \overline{w'q_t'^2}}{\partial z}}_{\text{transport}} - \underbrace{\frac{\overline{q_t'^2}}{\tau}}_{\text{dissipation}}$$

Simple (diagnostic)

$$M(q_t^{cu} - \overline{q_t}) \frac{\partial \overline{q_t}}{\partial z} \cong \frac{w_*^{cu}}{l_{cloud}} \overline{q_t'^2} \quad (\text{Lenderink and Siebesma 2000})$$

Works well but no memory: when convection dies out (night) => no variance => no clouds

Complex (prognostic): Tompkins 2002, Neggers 2007, Golaz 2003:

Extra closures needed (the shape of the pdf etc) looks promising implemented in 2 models (ECHAM, GFDL)

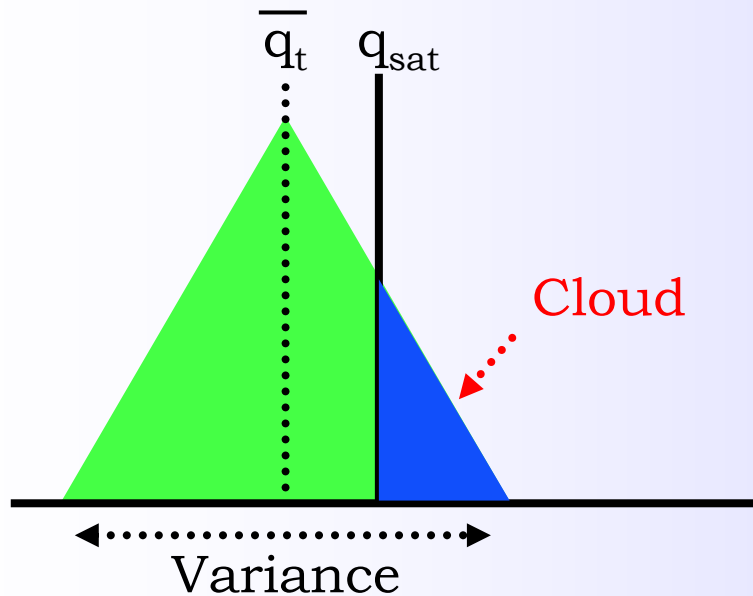
But what about cloud adjustment for ice clouds??

Prognostic statistical PDF scheme: Which prognostic variables/equations?

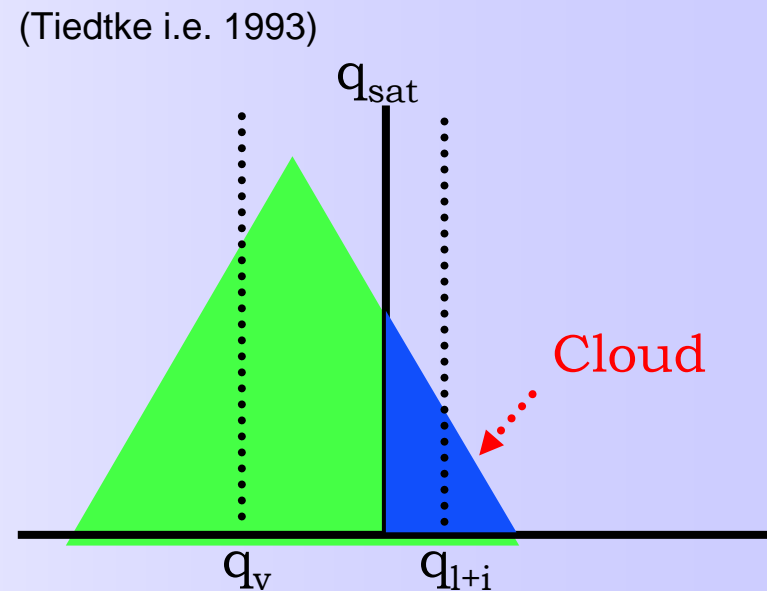
Taken from Forbes (ECMWF)

Take a 2 parameter distribution & partially cloudy conditions

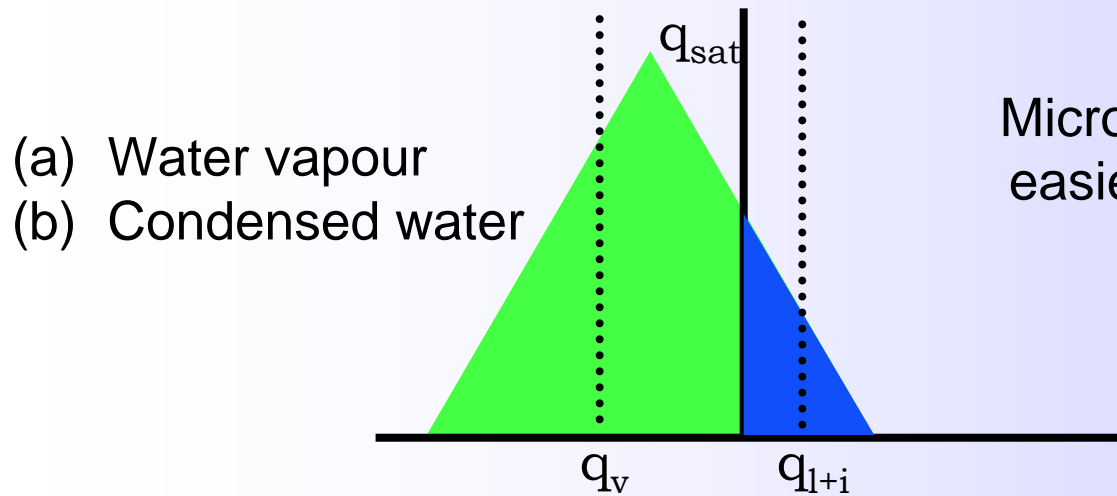
- (1) Can specify distribution with
 - (a) Mean
 - (b) Variance of total water



- (2) Can specify distribution with
 - (a) Water vapour
 - (a) Condensed water



Prognostic statistical scheme: (1) Water vapour and cloud water ?

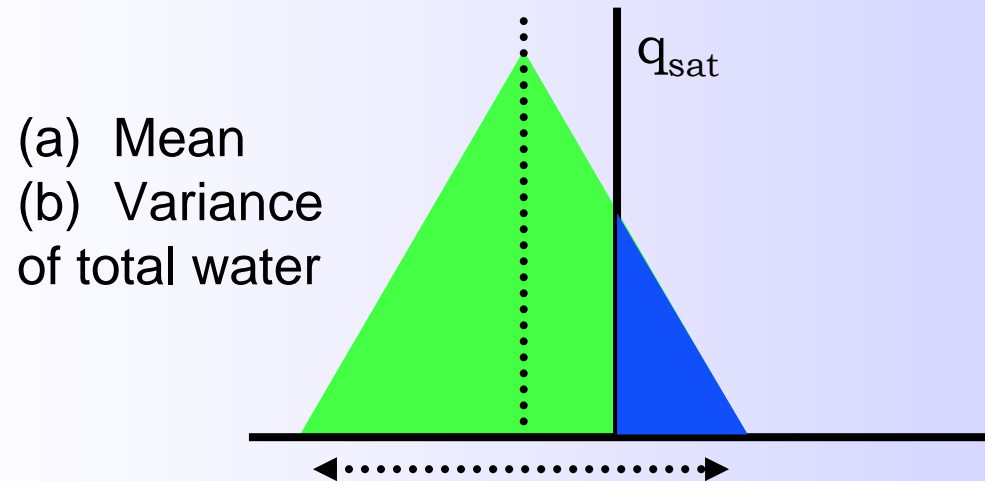


Microphysical sources and sinks
easier to parametrize.

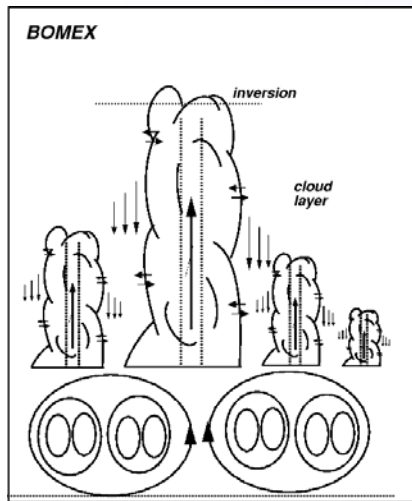
But problems arise in...

Finding the correct source and sink terms in the q_c equation

Prognostic statistical scheme: (2) Total water mean and variance ?



- “Cleaner solution”.
- Need to parametrize those tricky microphysics terms!



$$a_c = f\left(\frac{\bar{q}_t - \bar{q}_s}{\sigma_s}\right)$$

$$q_l = g\left(\frac{\bar{q}_t - \bar{q}_s}{\sigma_s}\right)$$

$$R(a_c, \bar{q}_t, \sigma_s)$$

Convection and turbulence parameterization give estimate of σ_s

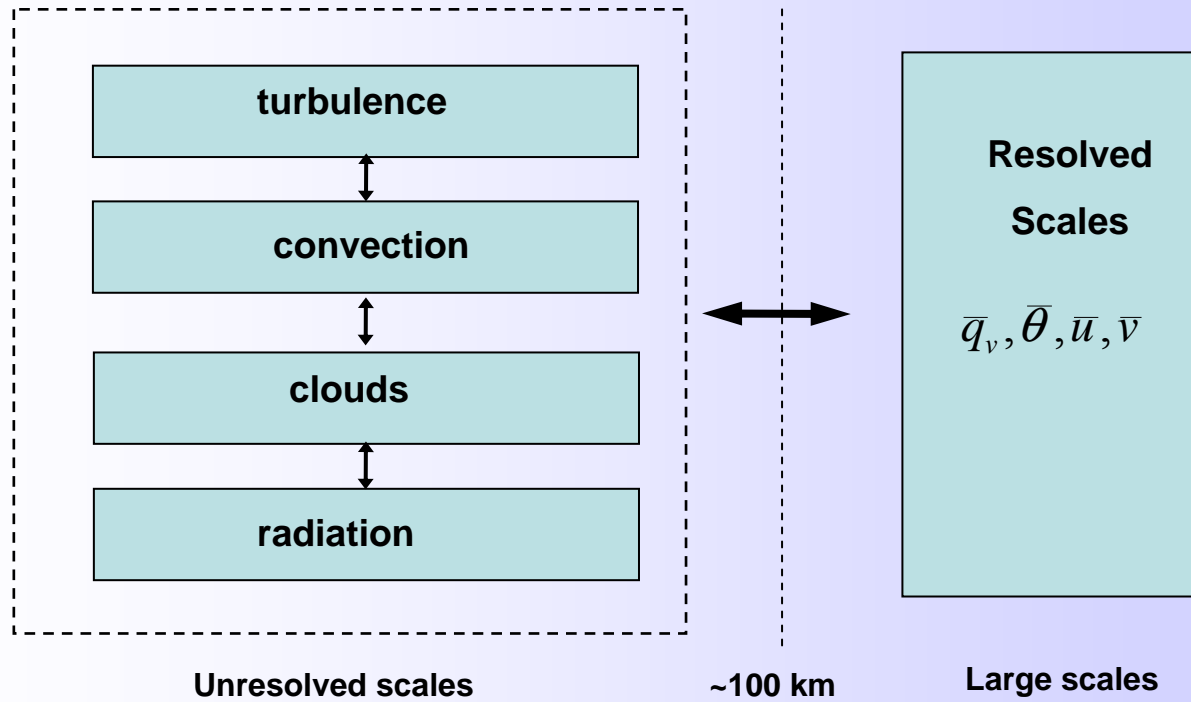
↔ **Cloud scheme :** ↔ **radiation scheme :**

- Schemes interact with each other on the subgrid scale
- **Subgrid variability (at least the 2nd moment) for the thermodynamic variables needs to be taken into account in any GCM for parameterizations of convection, clouds and radiation in a consistent way.**
- **At present this has not been accomplished in any GCM.**

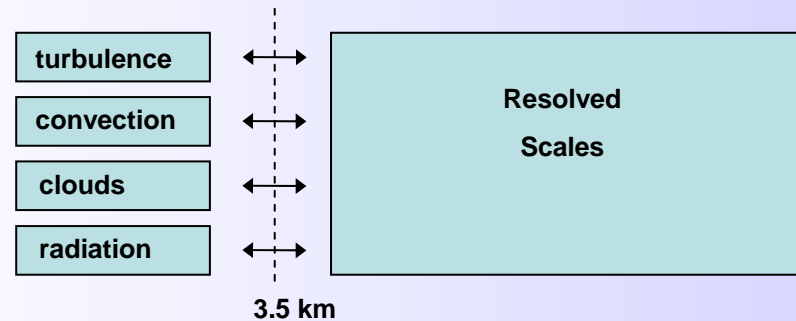
New Pathways



Consistent pdf based parameterizations



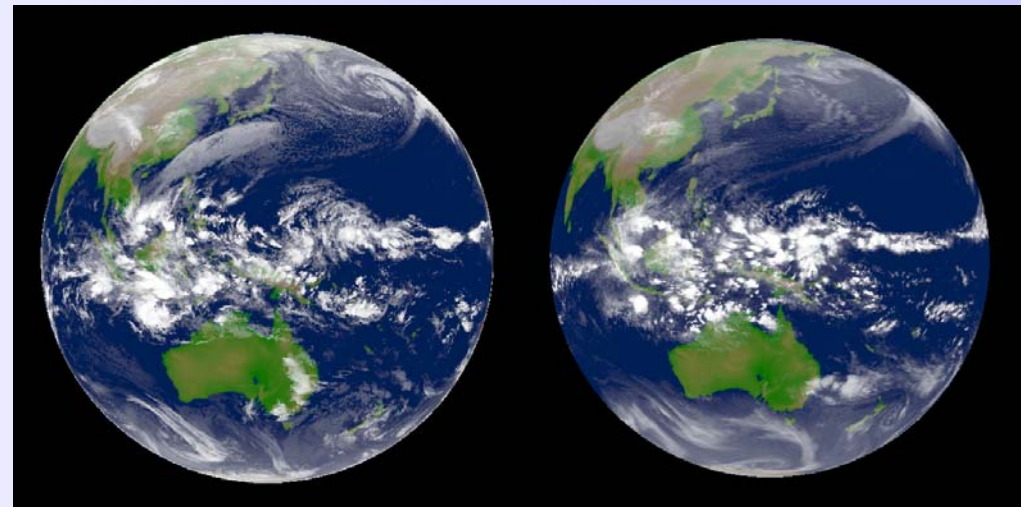
Pathway 1: Global Cloud Resolving Modelling (Brute Force)



NICAM simulation: MJO DEC2006 Experiment

3.5km run: 7 days from 25 Dec 2006

- *Short timeslices*
- *Testbed for interactions:
deep convection and the large scale*
- *Boundary clouds, turbulence,
radiation still unresolved*

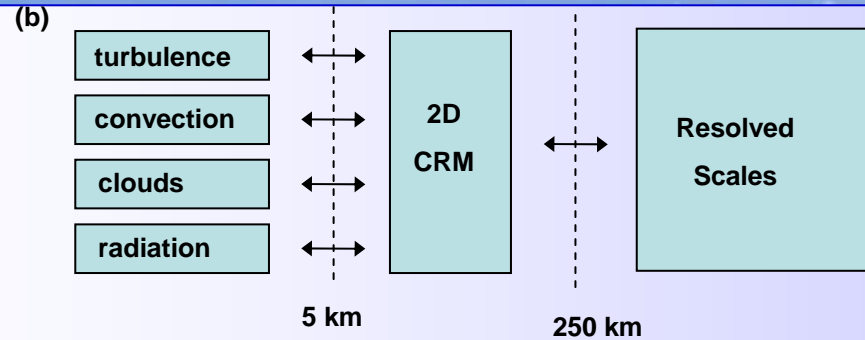


MTSAT-1R

NICAM 3.5km

Miura et al. (2007, Science)

Pathway 2: Superparameterization

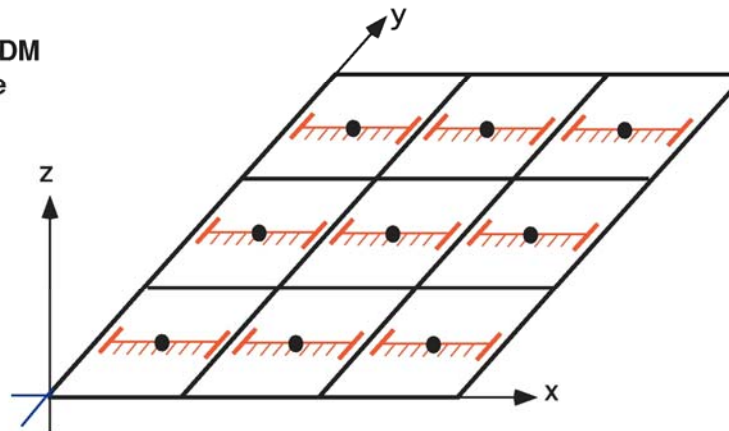


Cloud-Resolving Convection Parameterization or Super-Parameterization

Grabowski (2001), Khairoutdinov and Randall (2001)

Application of
a 2D CSRM within each column of a large-scale dynamical model (LSDM)
with periodic lateral boundary conditions

At the ● points, the LSDM
and the domain-average
of the CSRM interact.



Concept and viewgraph from Akio Arakawa

Pathway 2: Superparameterization



What do we get?

- *Explicit deep convection*
- *Explicit fractional cloudiness*
- *Explicit cloud overlap and possible 3d cloud effects*
- *Convectively generated gravity waves*

But.....

A GCM using a super-parameterization is three orders of magnitude more expensive than a GCM that uses conventional parameterizations.

On the other hand super-parameterizations provide a way to utilize more processors for a given GCM resolution

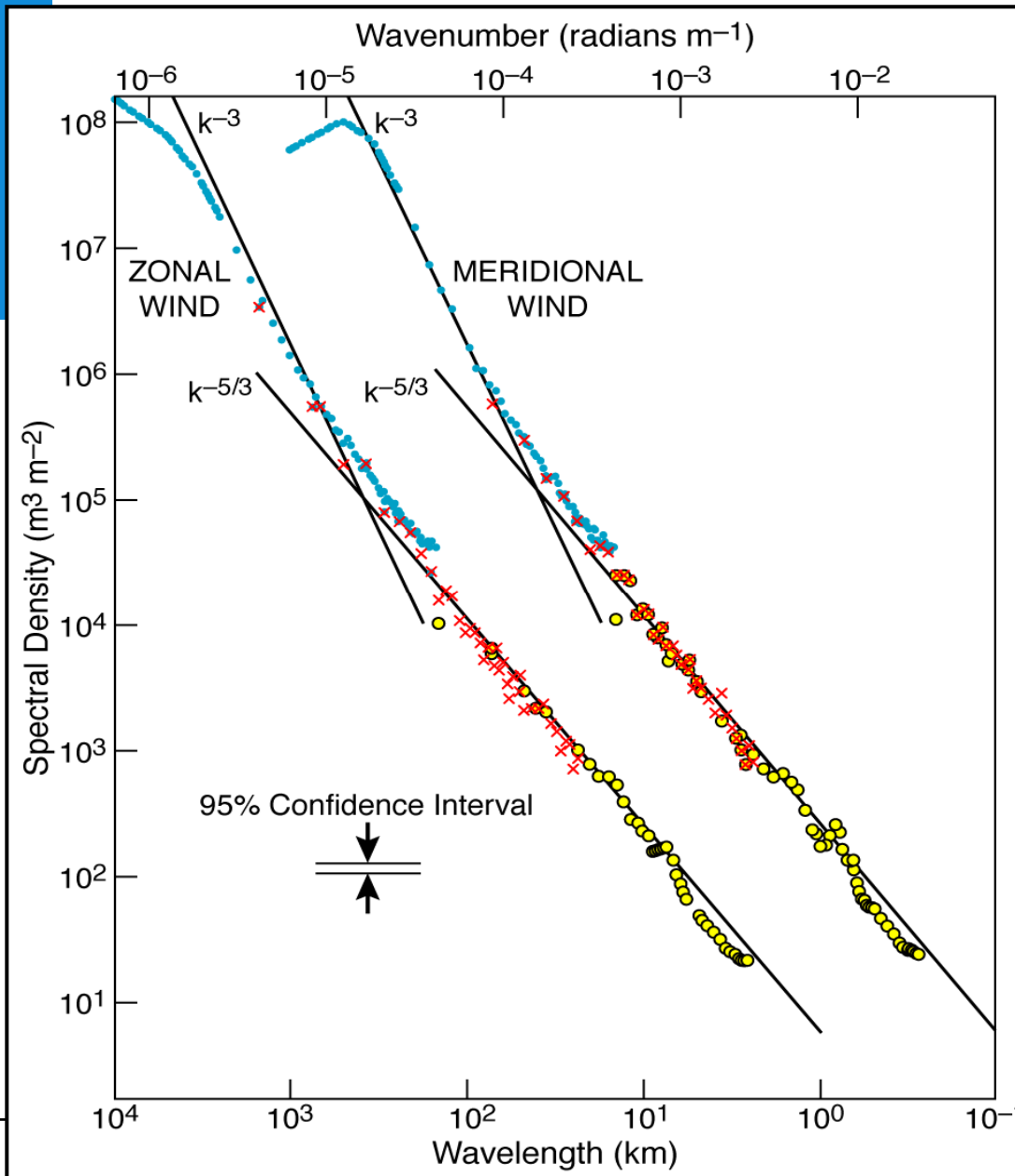
Boundary Layer Clouds, Microphysics and Turbulence still needs to be parameterized

2D?

5.

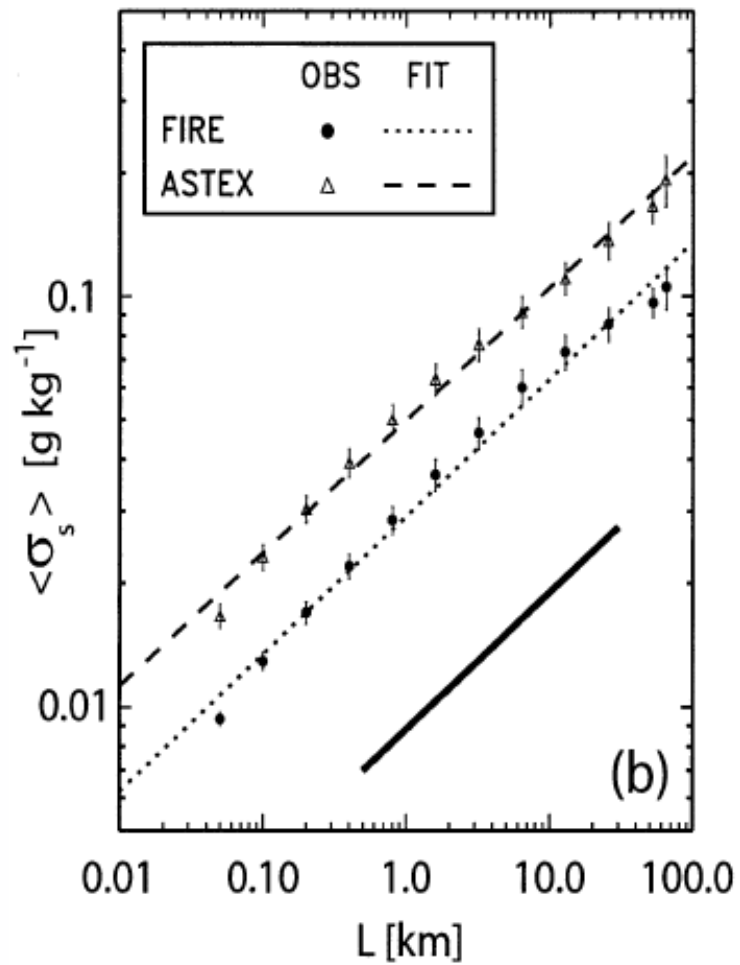
Scale Aware and Stochastic Parameterizations

Kinetic energy spectra from aircraft



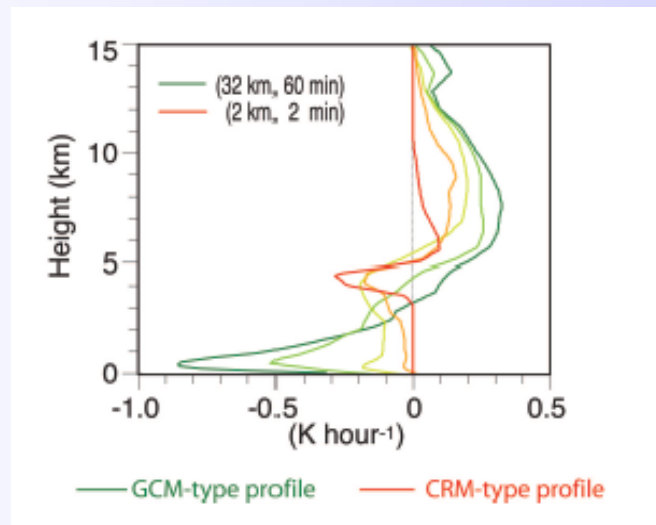
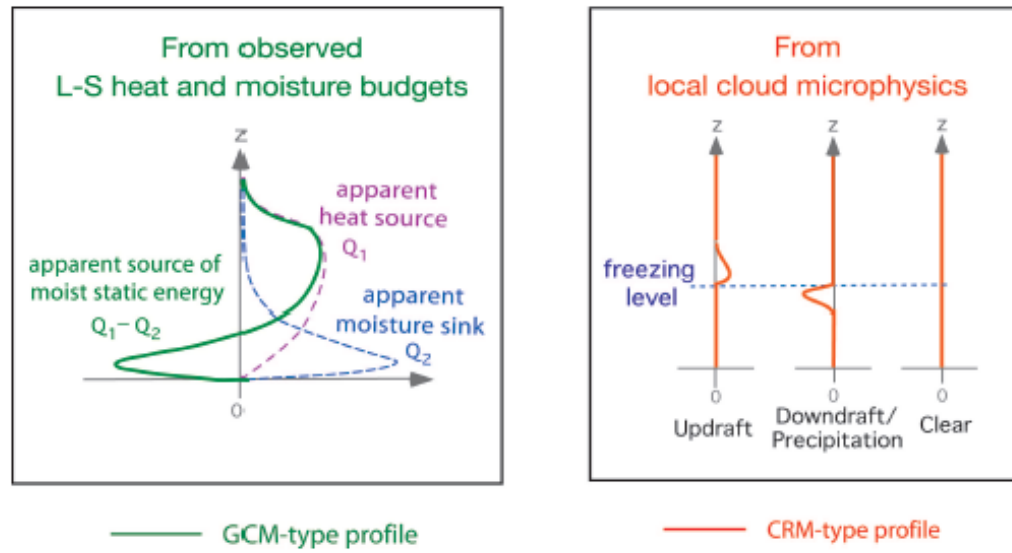
No Spectral Gap!!!

Similar for variance of temp and humidity



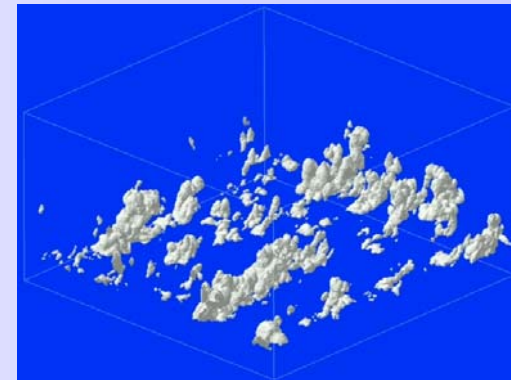
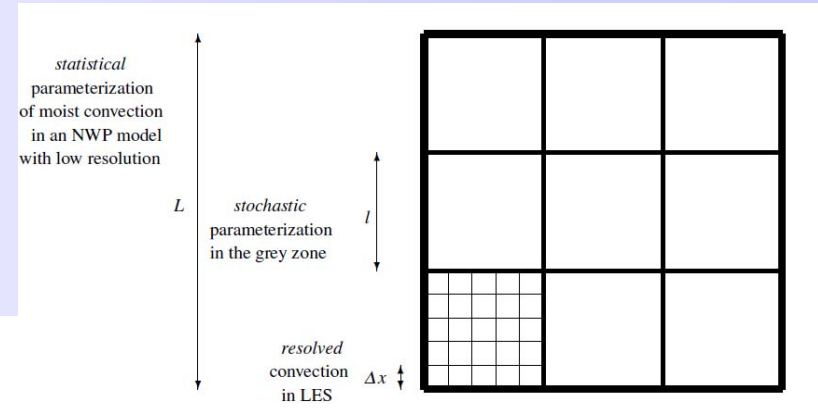
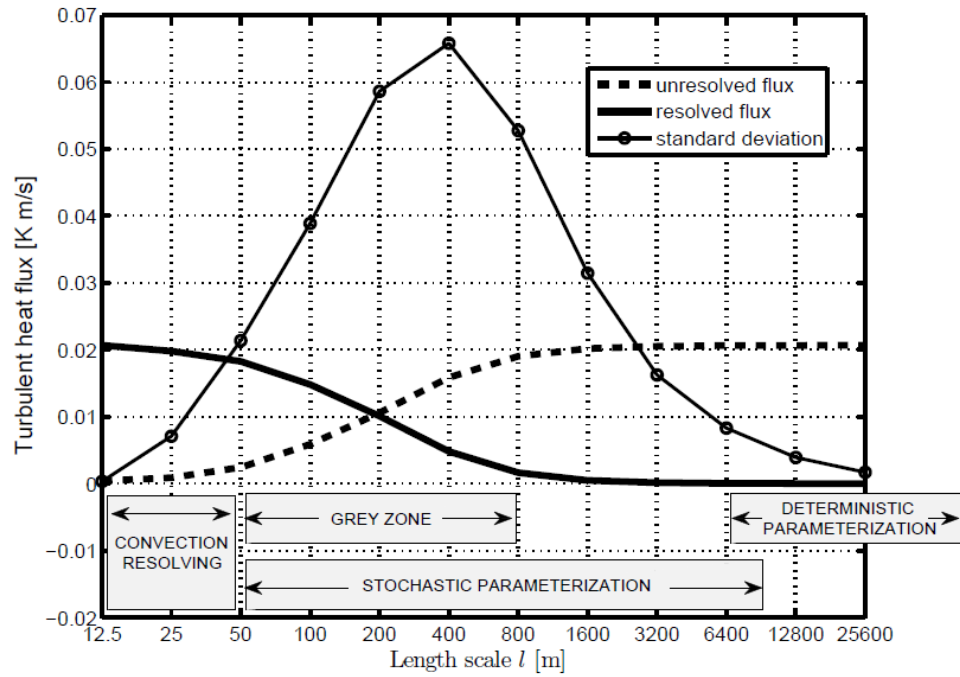
Cloud schemes: $\sigma_s = \sigma_s(l)$

Convection schemes: deep convection



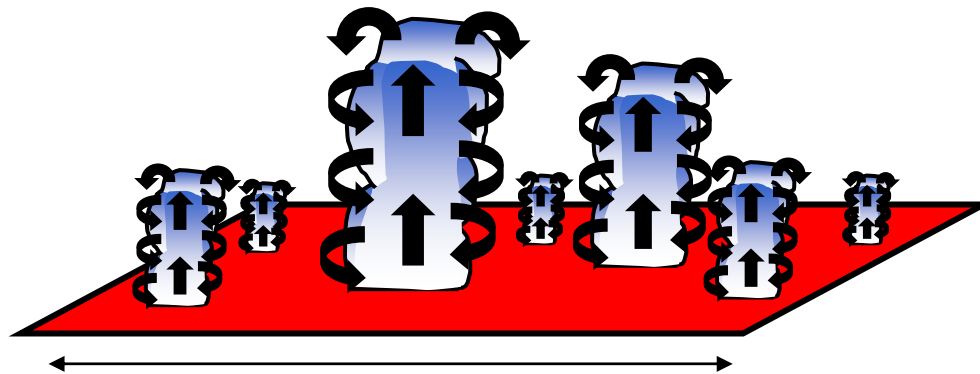
Convection schemes: shallow convection

Dorrestijn, Siebesma, Crommelin, Jonker, 2012



Deterministic versus Stochastic Convection (1)

- Traditionally convection parameterizations are deterministic:
 - Instantaneous grid-scale flow and mean state is taken as input and convective response is deterministic
 - One to one correspondency between sub-grid state and resolved state assumed.
 - Conceptually assumes that spatial average is a good proxy for the ensemble mean.
 - This assumption breaks down at higher resolutions

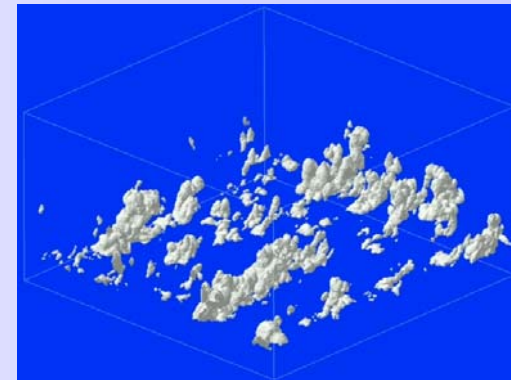
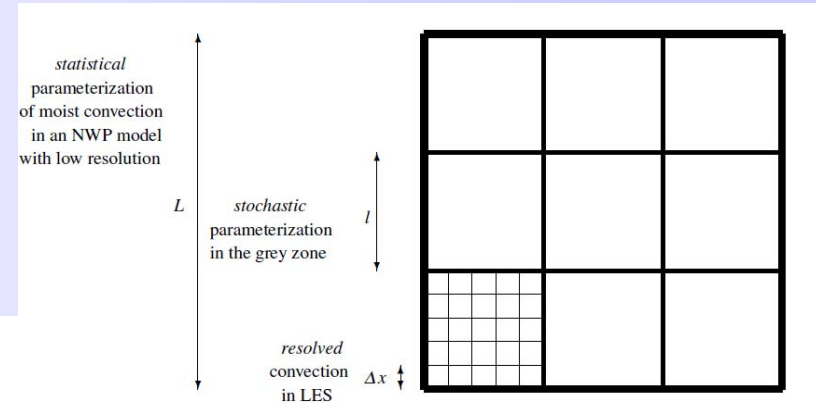
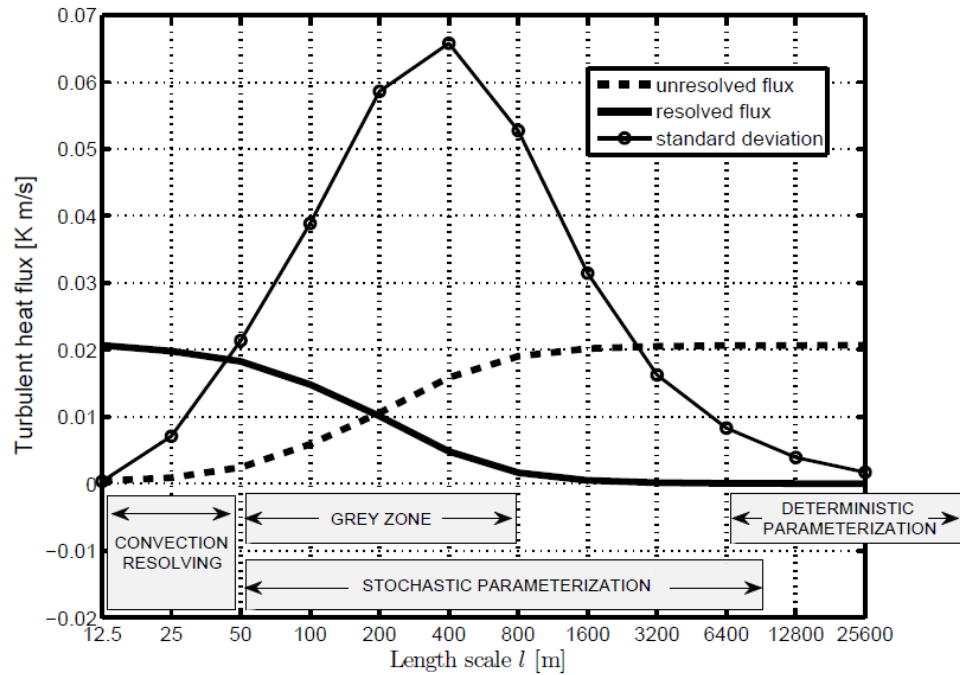


~500k
m



Stochastic Noise happens especially in the Grey Zone

Dorrestijn, Siebesma, Crommelin, Jonker, 2012



All the new pathways are exciting and are happening now!

Parameterization is really about understanding cloud processes and their interaction with the large scale so: